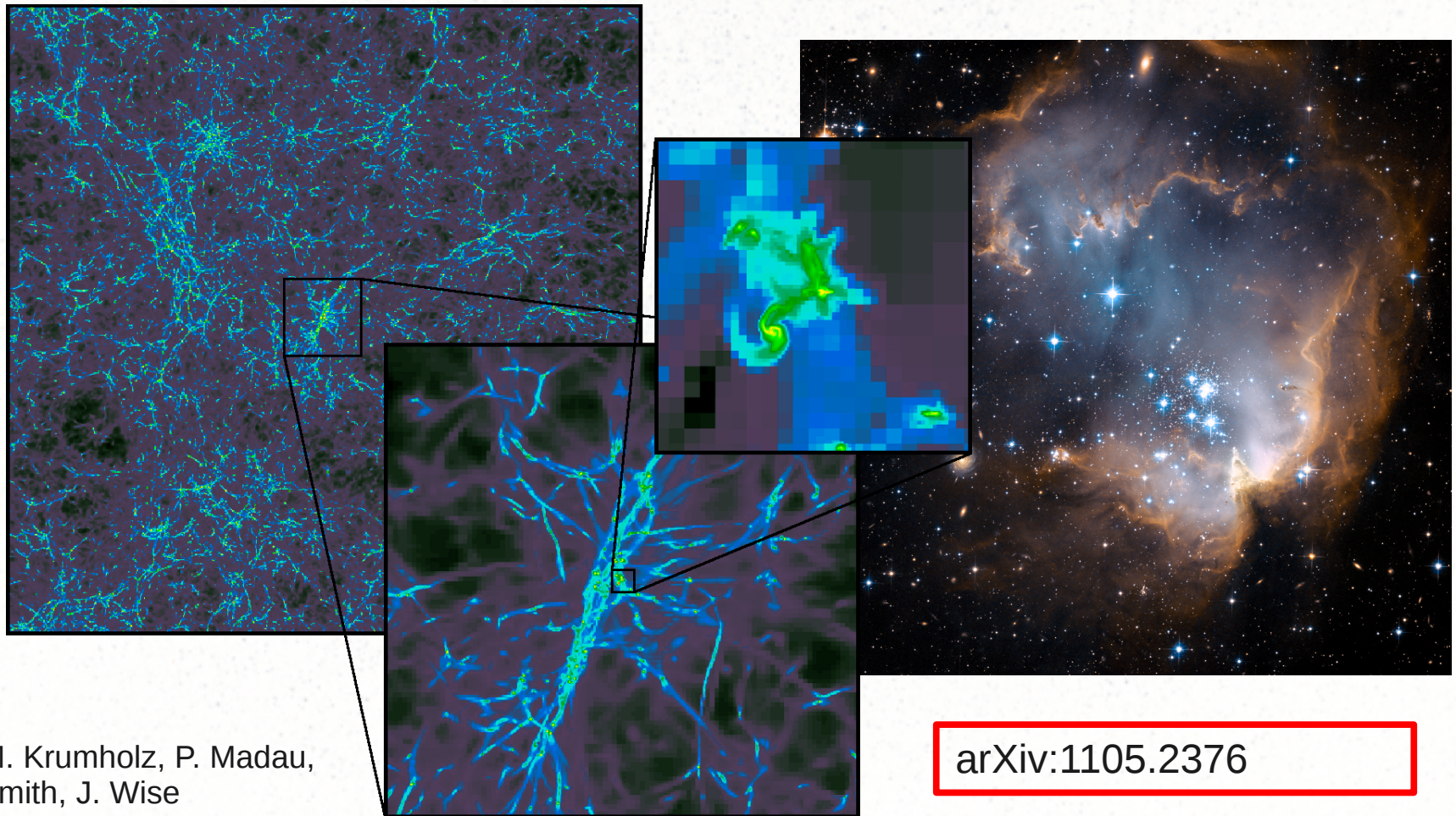


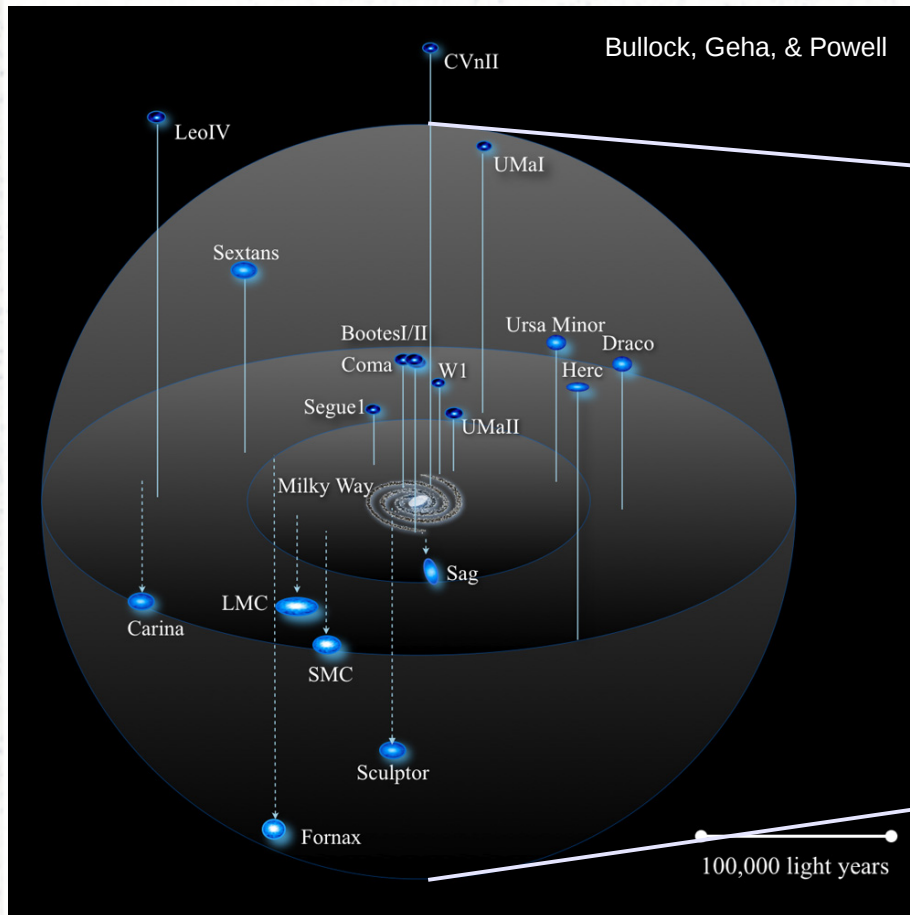
Dwarf Galaxy Formation with H_2 -regulated Star Formation

Michael Kuhlen, UC Berkeley

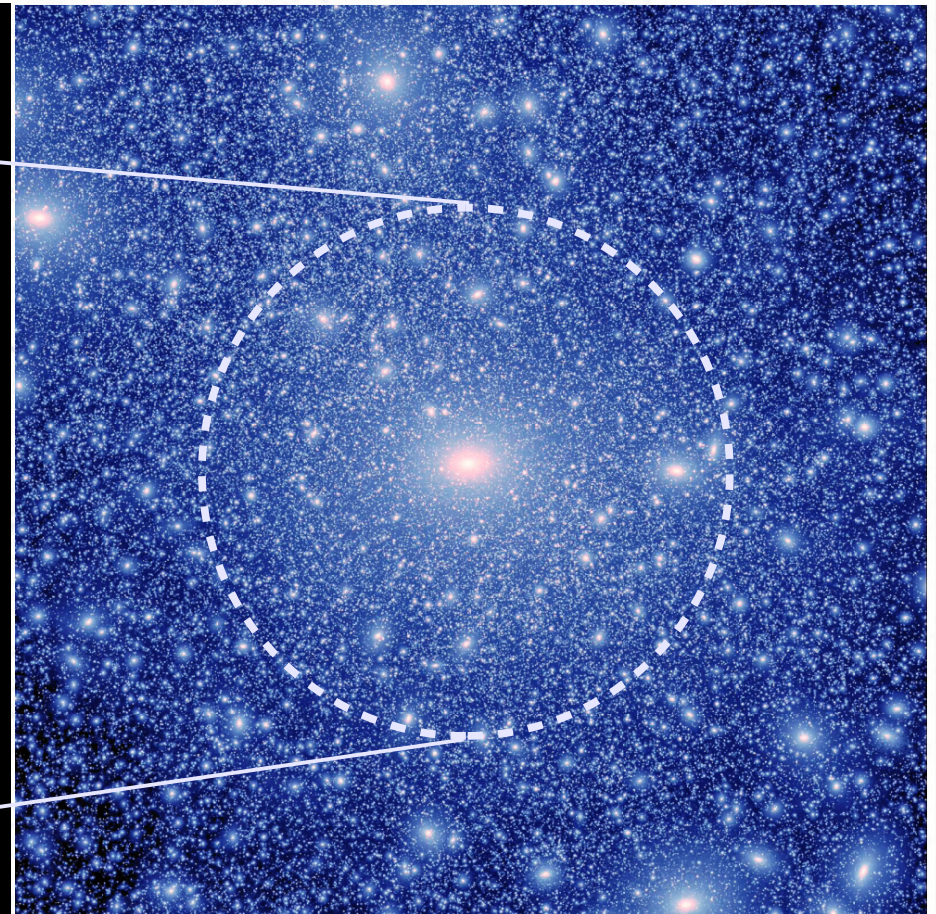


The Missing Satellites Problem

Reality



Dark Matter Simulation

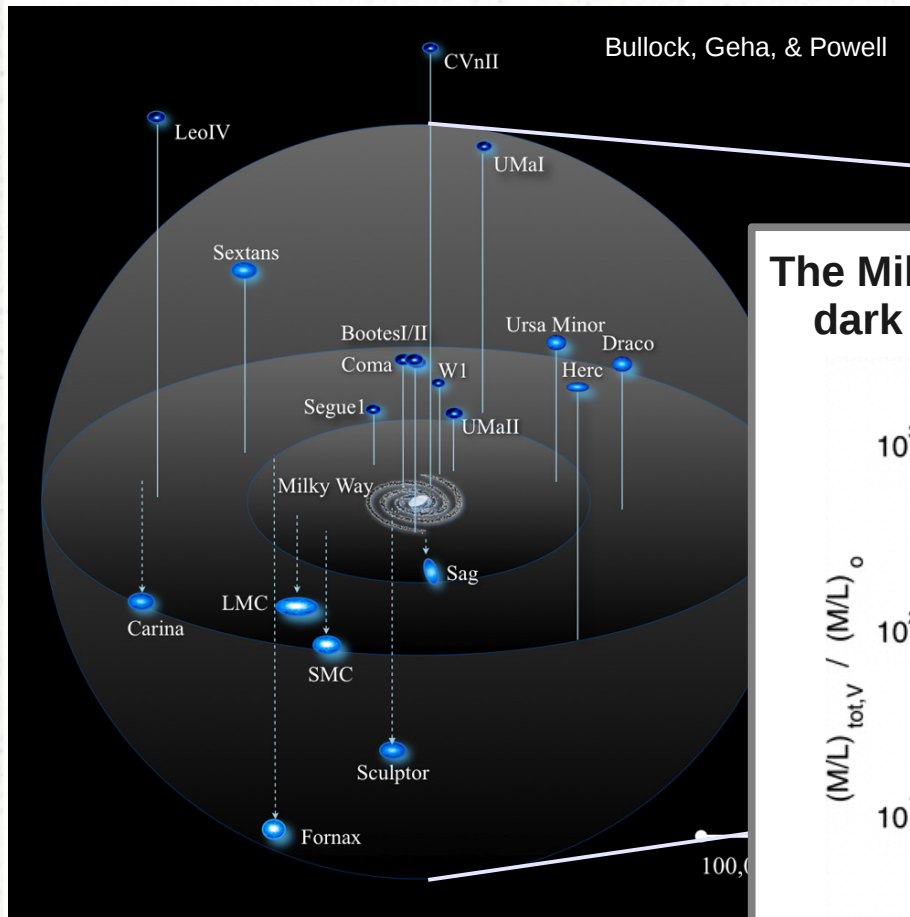


There is strong tension between the observed number of dwarf satellite galaxies and the predicted number of dark matter subhalos orbiting our Milky Way galaxy.

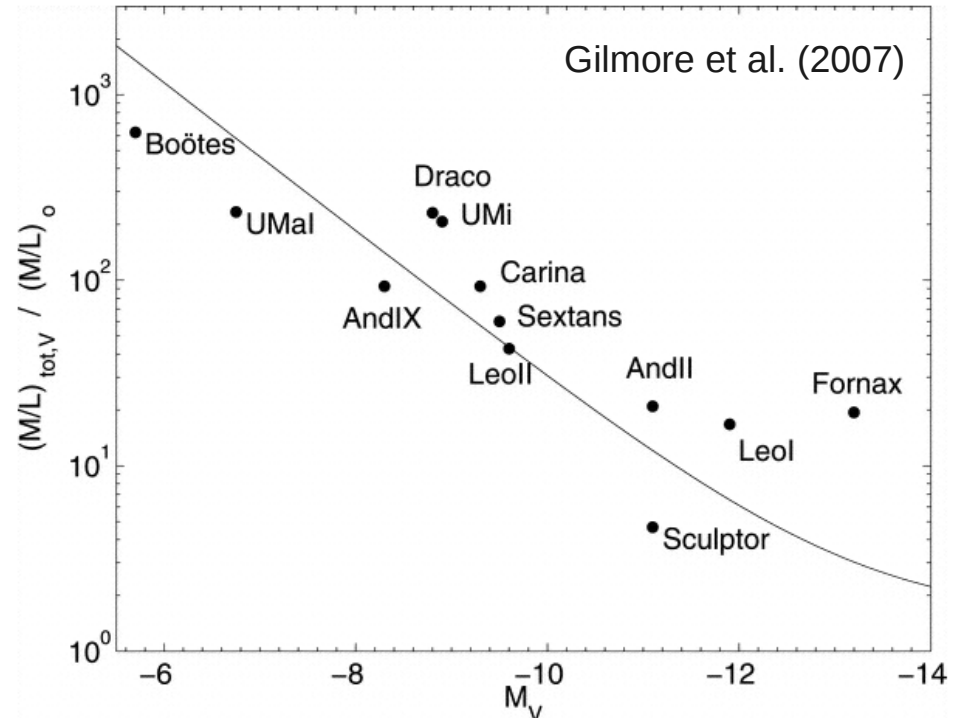
The Missing Satellites Problem

Reality

Dark Matter Simulation



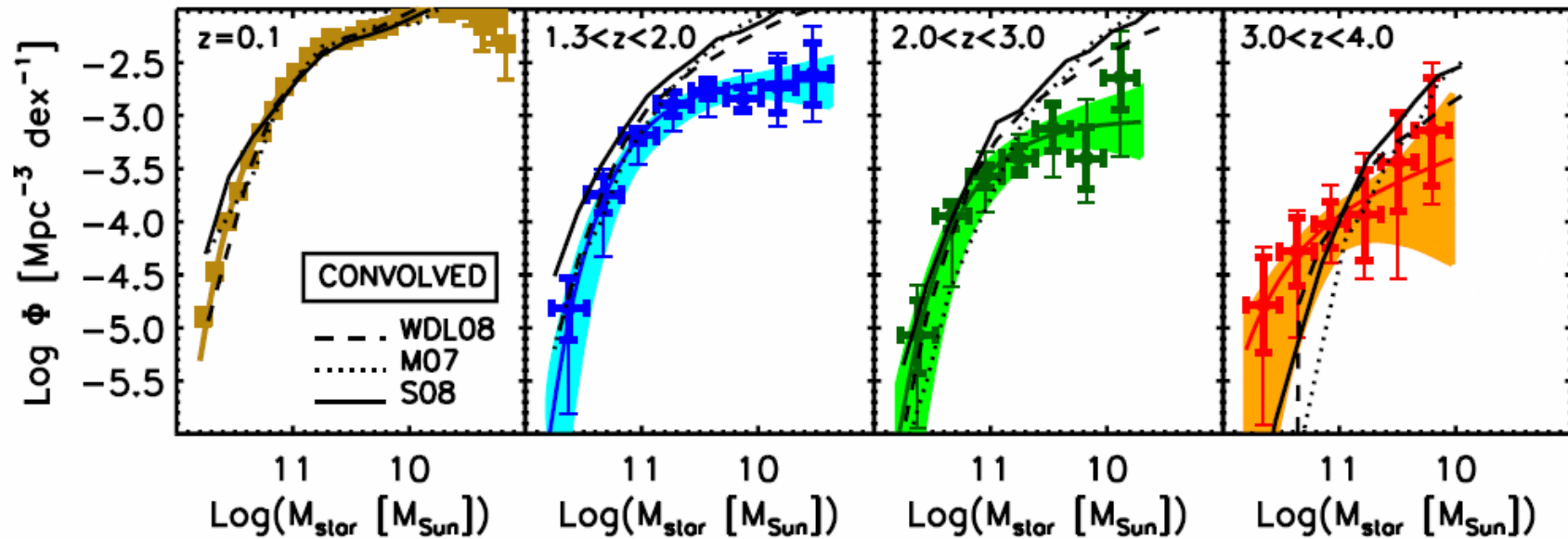
The Milky Way dwarf satellite galaxies are the most dark matter dominated objects in the universe!



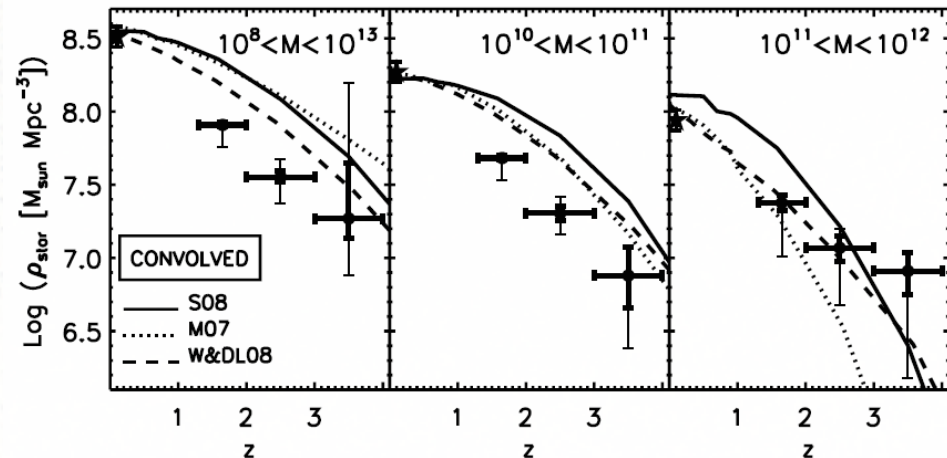
There is strong tension between
and the predicted number of da

The Field Dwarf Galaxy Problem

Marchesini et al. (2009) [see also Fontanot et al. 2009, Cirasuolo et al. 2010]

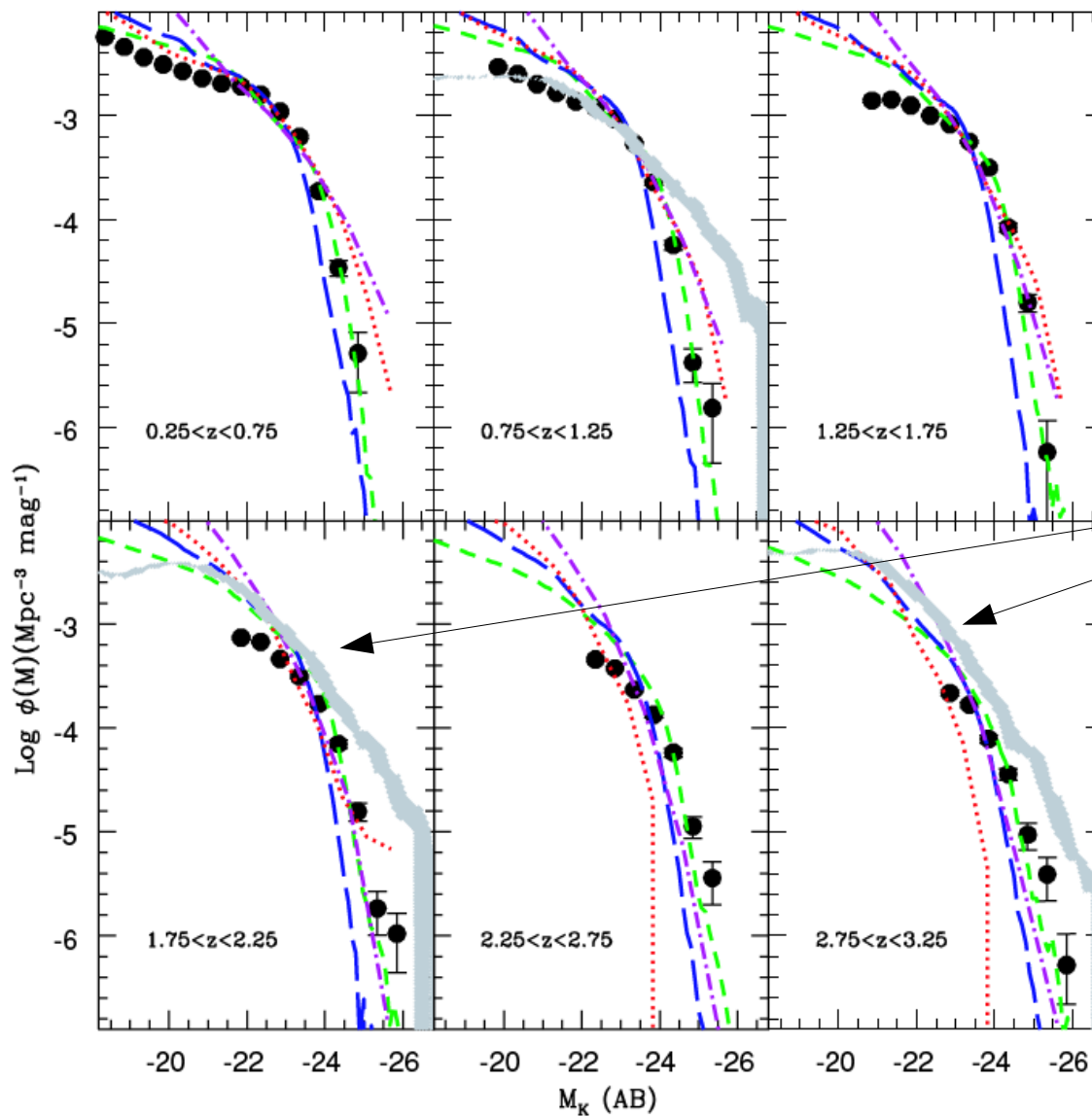


Semi-analytic models of galaxy formation (including prescriptions for SN feedback!) **over-predict the abundance of low mass galaxies and the stellar mass density at intermediate to high redshifts.**



The Field Dwarf Galaxy Problem

from Cirasuolo et al. 2010



Similar problems for hydrodynamic galaxy formation **simulations** including SN feedback.

Hydro Simulations:
Cen & Ostriker (2006)
Nagamine et al. (2006)

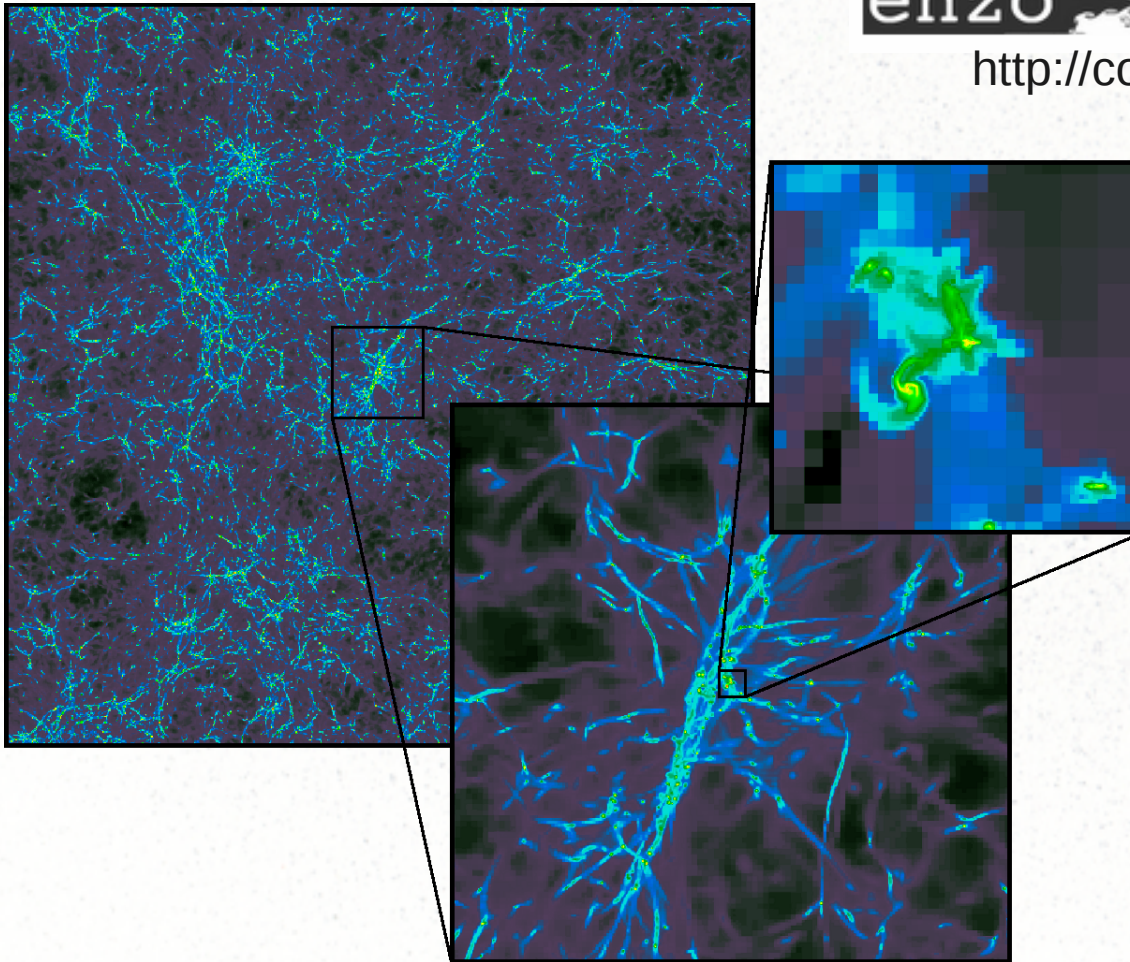
Hydrodynamical Galaxy Formation Simulations

enzo

enzo

Astrophysical Adaptive Mesh Refinement

<http://code.google.com/p/enzo/>



- Cosmological Adaptive Mesh Refinement
- Follows dark matter and hydrodynamics.
- Includes cooling, star formation, supernova feedback, etc.
- **Community code**
- I've been a contributing developer since 2005.

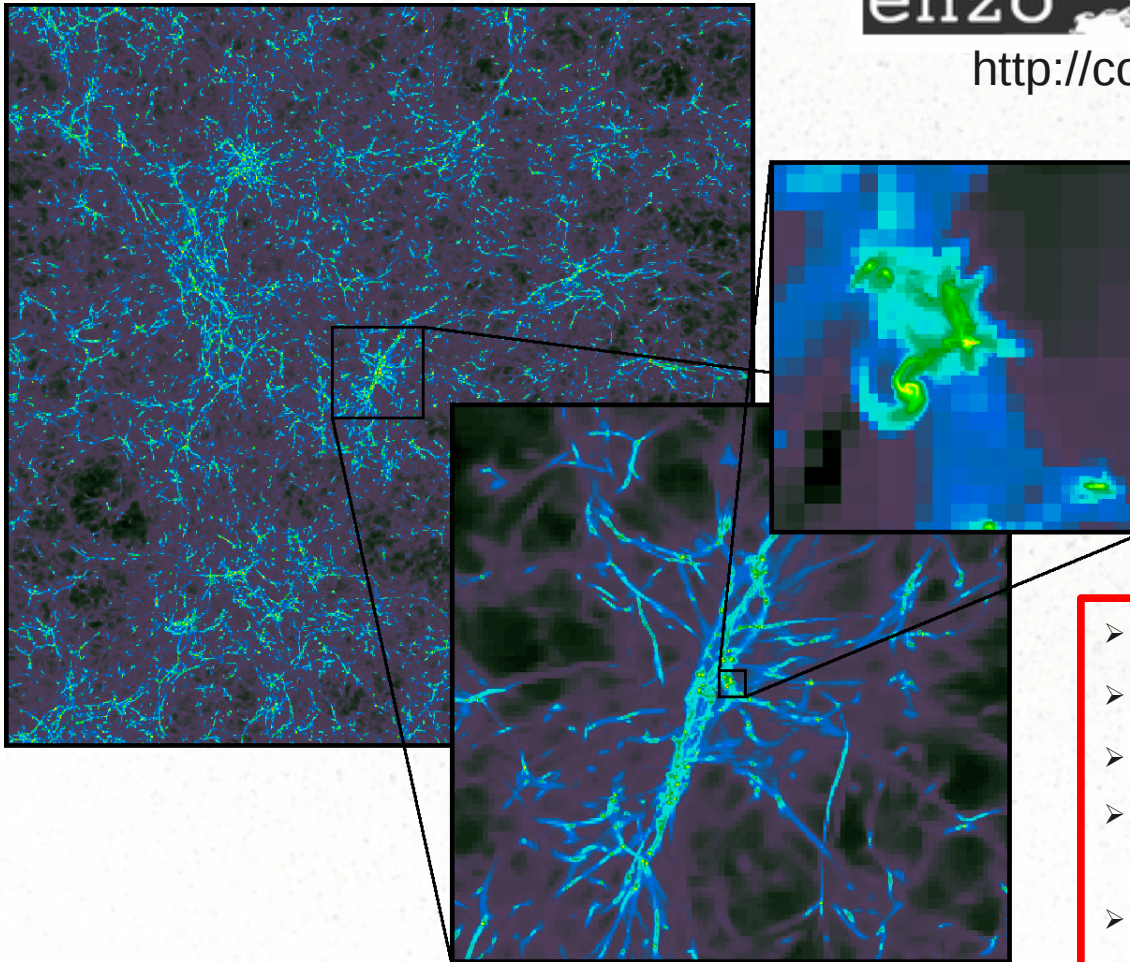
Hydrodynamical Galaxy Formation Simulations

enzo

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Astrophysical Adaptive Mesh Refinement

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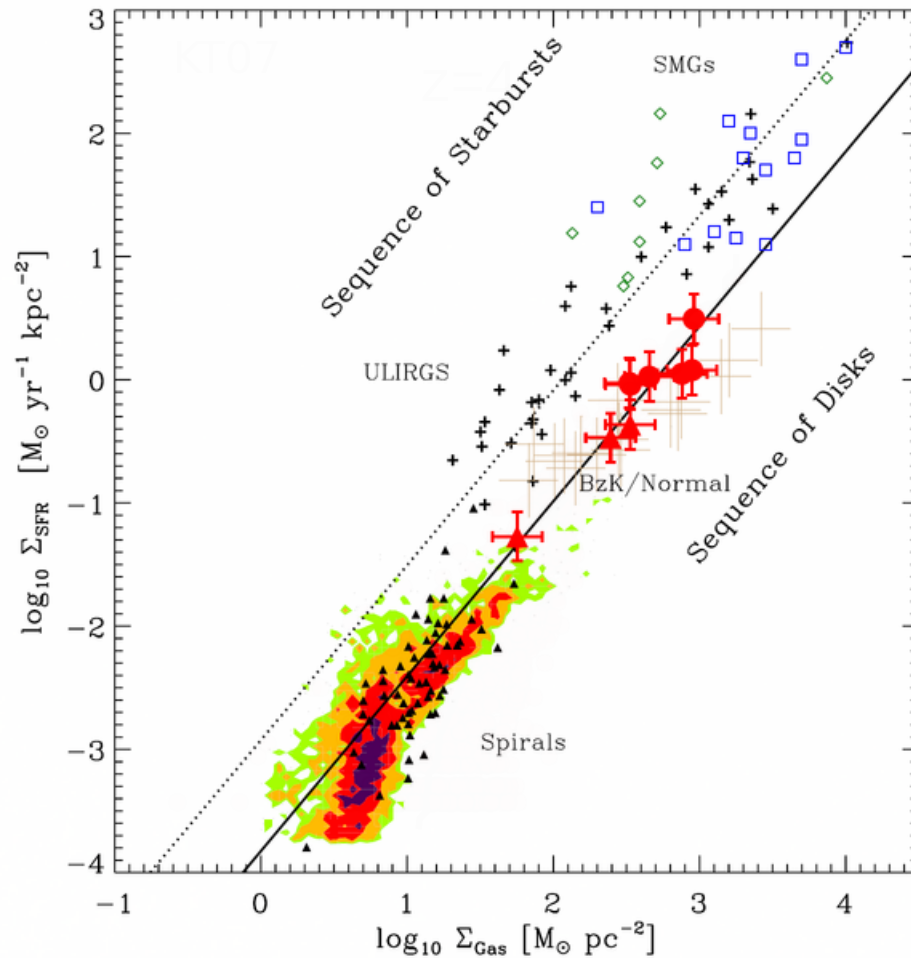


- Cosmological Adaptive Mesh Refinement
- Follows dark matter and hydrodynamics.
- Includes cooling, star formation, supernova feedback, etc.
- **Community code**
- I've been a contributing developer since 2005.

- 12.5 Mpc box
- 256^3 DM particles ($3 \times 10^6 M_{\odot}$)
- 256^3 root grid + 7 levels of AMR
- $\Delta x = 54.5 \times 7/(1+z) \times 2^{7-\text{level}}$ proper pc
- Self-consistent metal cooling
- **H₂-regulated star formation**

“Standard” Star Formation Simulation

Daddi et al. (2010)



Krumholz & Tan (2007) model

Constant SFR per free-fall time

SF threshold: $n_{\text{thresh}} = 50 \text{ cm}^{-3}$

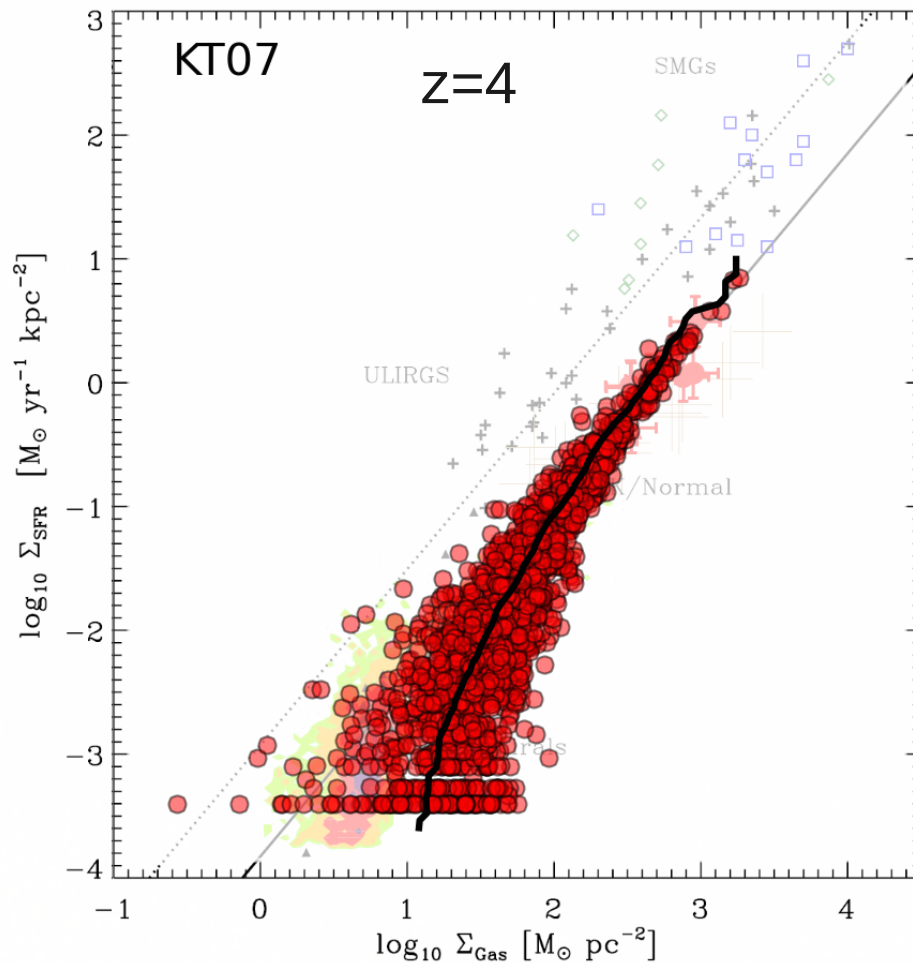
$$\dot{\rho}_{\text{SF}} = \epsilon_{\star} \frac{\rho_{\text{gas}}}{t_{\text{freefall}}} \propto \rho_{\text{gas}}^{3/2}$$

$$t_{\text{freefall}} = \sqrt{\frac{3\pi}{32G\rho}}$$

$$\epsilon_{\star} = 0.01$$

Kuhlen, Krumholz, Madau, Smith, Wise (2011, arXiv:1105.2376)

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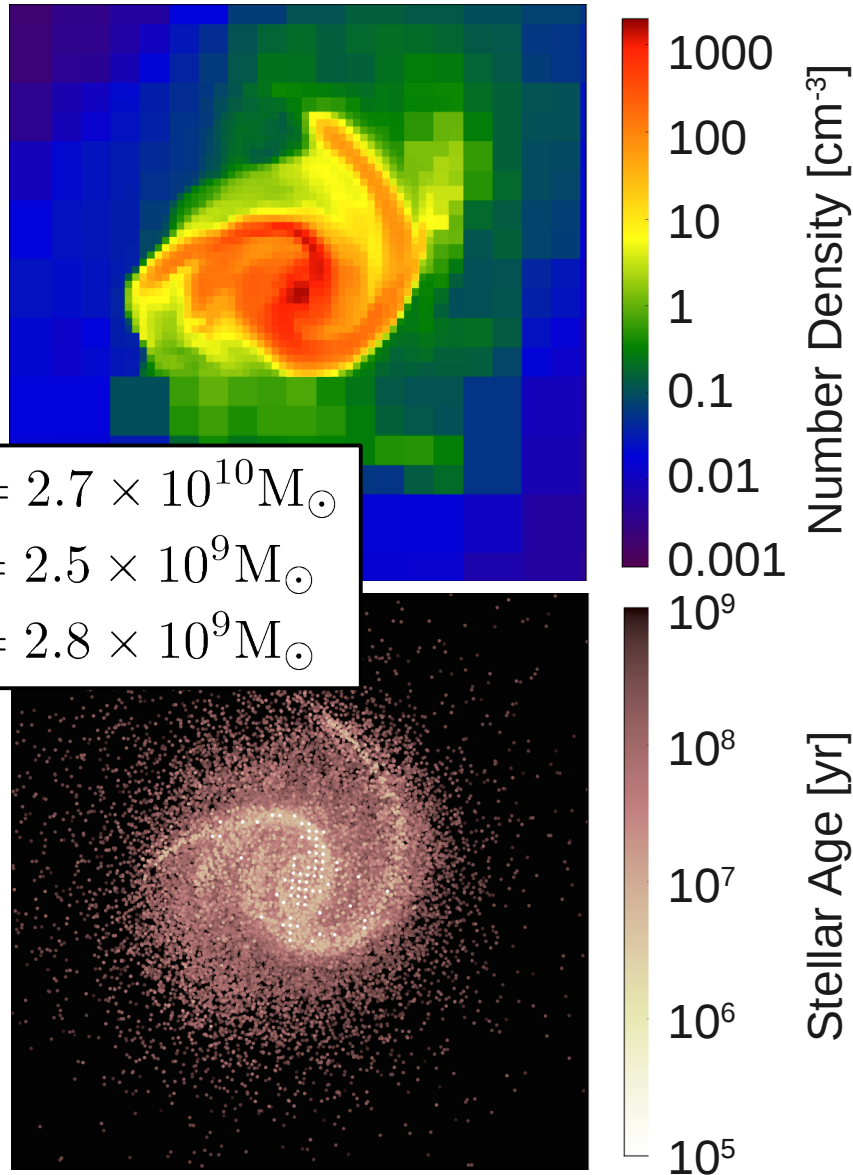
$$t_{\text{freefall}} = \sqrt{\frac{3\pi}{32G\rho}}$$

$$\epsilon_{\star} = 0.01$$

$$\text{SFR}_{\text{ff-X}} = \frac{f_X \dot{M}_{\star} t_{\text{ff-X}}}{M_X}$$

Kuhlen, Krumholz, Madau, Smith, Wise (2011, submitted)

“Standard” Star Formation Simulation



$$\begin{aligned} M_{\text{tot}} &= 2.7 \times 10^{10} M_{\odot} \\ M_{\text{gas}} &= 2.5 \times 10^9 M_{\odot} \\ M_{\star} &= 2.8 \times 10^9 M_{\odot} \end{aligned}$$

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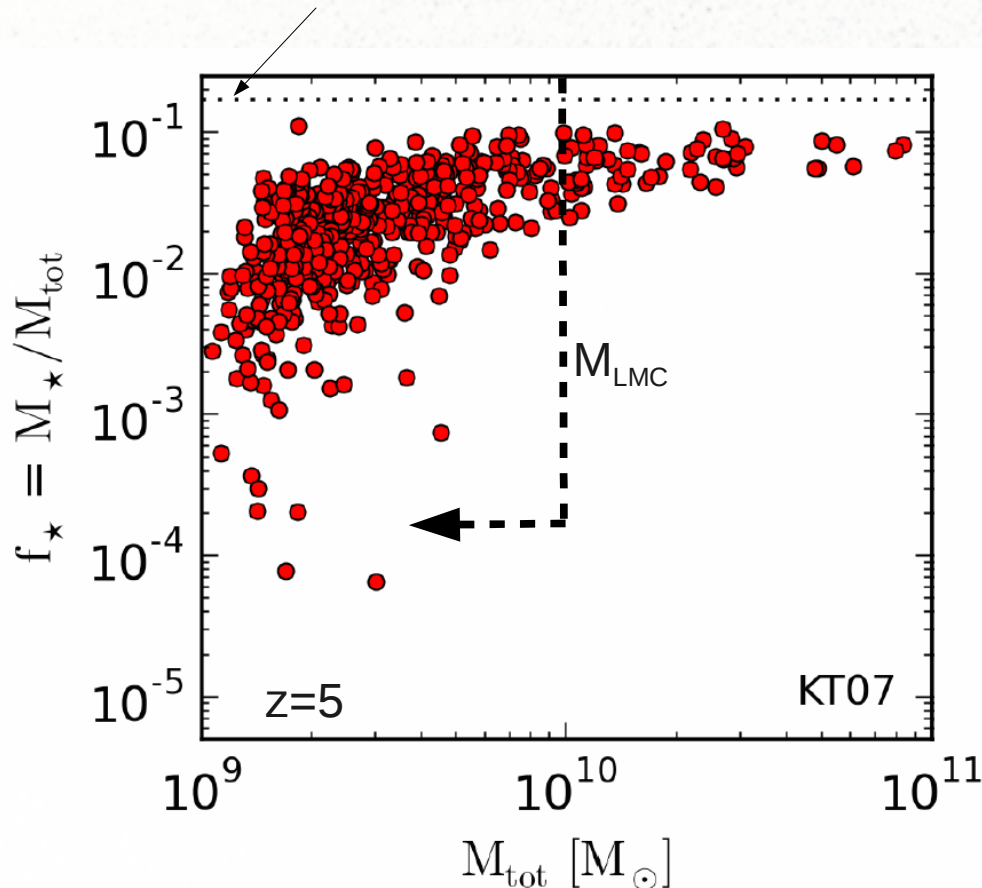
$$\epsilon_{\star} = 0.01$$

Only **weak supernova feedback**:

- Injection of thermal energy ($\epsilon=10^{-5}$) in central grid cell.
- No winds!

Stellar Mass Fraction Too High in Low Mass Halos

($f_{\star} = \Omega_b$, i.e. 100% gas to star conversion)



Krumholz & Tan (2007) model

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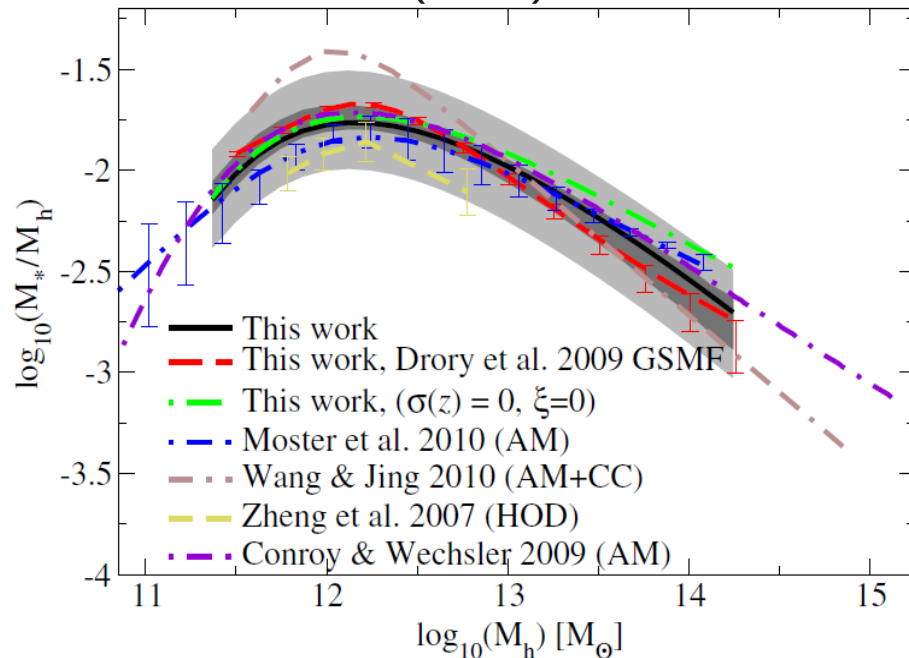
Star formation efficiency is too high in low mass halos!

This would greatly overproduce the dwarf galaxy luminosity/mass function.

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Behroozi et al. (2010)



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How to suppress SF in low mass halos

The most commonly invoked mechanism to suppress star formation in low mass dark matter halos is **Supernova/Stellar Wind Feedback** and **UV Photoheating**.

1) UV Photoheating

- Typically only effective below few $\times 10^9 M_{\odot}$ halos.
- Difficult to explain complicated SF histories if Milky Way dwarfs

2) Supernova/Stellar Wind Feedback

- Undoubtedly plays an important role in nature!
- Its effectiveness in numerical simulations is very implementation dependent.
- Even hydro simulations with SN feedback have trouble matching observed stellar mass functions.
- In SAMs it typically just means a removal of some/all gas from the SF reservoir below some halo mass, or a halo-mass-dependent SF efficiency.

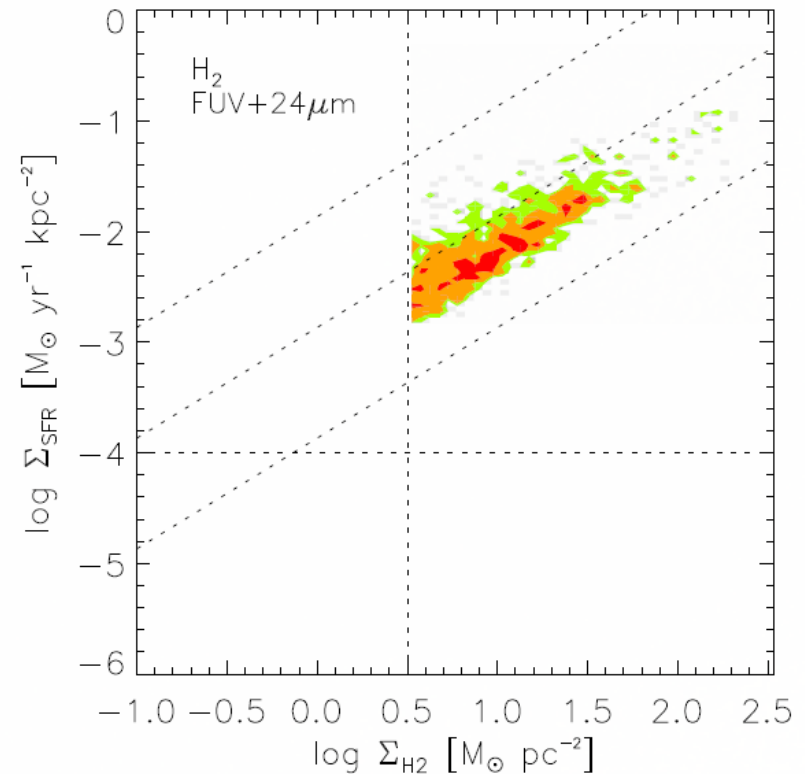
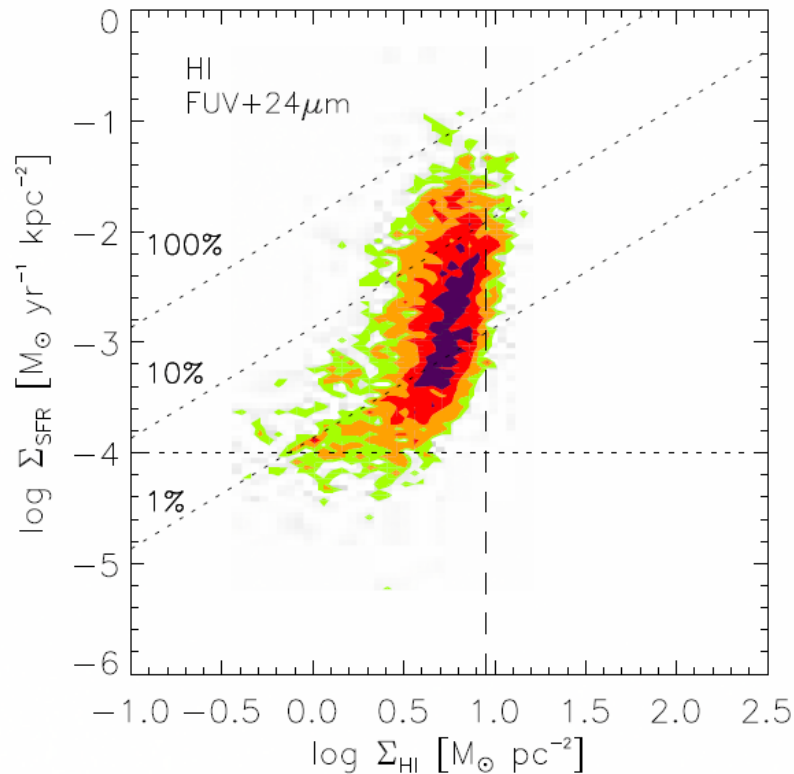
Is it the whole story? Are we just putting the answer we want in by hand? In my opinion other mechanisms should be considered...

For example: Molecular Hydrogen Regulated Star Formation.

cf. Gnedin et al. (2009), Gnedin & Kravtsov (2010, 2011)

H₂-regulated Star Formation

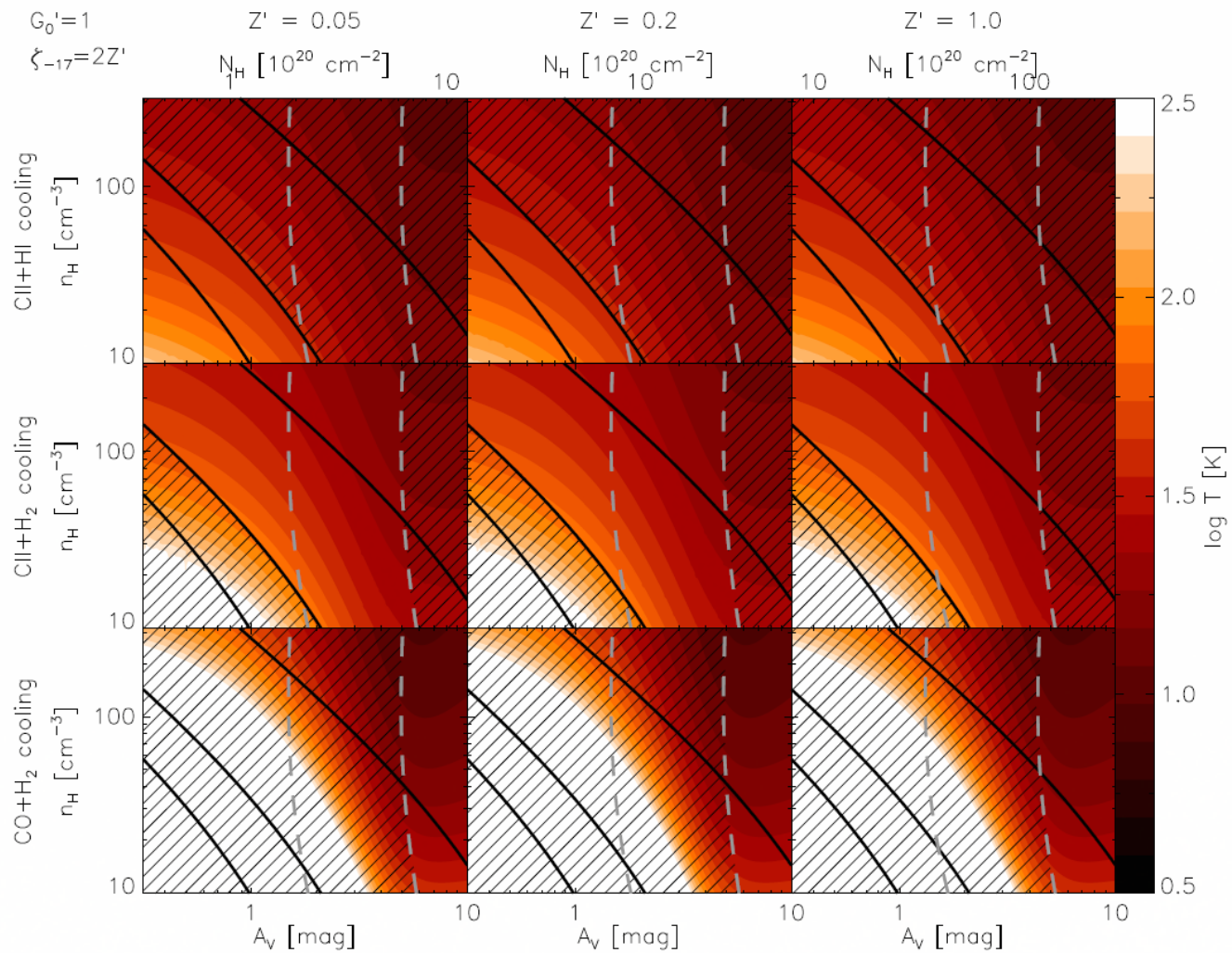
Bigiel et al. (2008): observational Kennicutt-Schmidt relation from spatially resolved (< 1 kpc) **radio, IR, and UV** observations of 7 nearby spiral galaxies.



The star formation rate correlates better with molecular gas (H₂) than with atomic gas (HI) surface density.

H₂-regulated Star Formation

SFR correlates with H₂ even though it's not the primary coolant (CII, CO)!



Krumholz, Leroy, & McKee (2011)

H₂-regulated Star Formation

Pelupessy et al. (2006), Robertson & Kravtsov (2008), Gnedin et al. (2009), Feldmann et al. (2010), Krumholz & Gnedin (2010)

Make SFR proportional to ρ_{H_2} : $\dot{\rho}_{\text{SF}} = \epsilon_{\star} \frac{\rho_{\text{H}_2}}{t_{\text{freefall}}} \propto f_{\text{H}_2} \rho_{\text{gas}}^{3/2}$

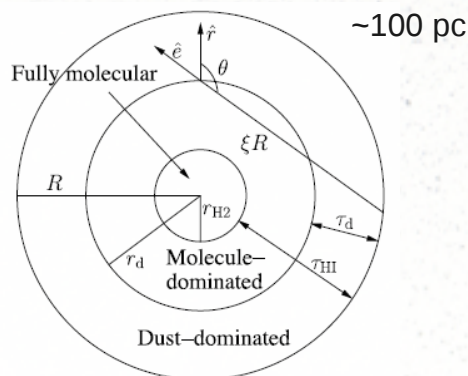
How to get f_{H_2} during simulation runtime:

- 1) Full non-equilibrium chemistry with H₂ formation on dust grains, coupled to radiation transfer with Lyman Werner shielding (e.g. Gnedin et al. 2009, Feldman et al. 2010).
- 2) Use results from idealized 1-D RT calculations of H₂ formation-dissociation balance in giant atomic-molecular cloud complexes (KMT09: Krumholz, McKee, & Tumlinson (2008, 2009), McKee & Krumholz (2010)).

Radiative transfer: $\hat{e} \cdot \nabla I_{\nu} = -n \left(\frac{1}{2} f_{\text{H}_2} \sigma_{\text{H}_2, \nu} + \sigma_{d, \nu} \right) I_{\nu}$

H₂ formation-dissociation

balance: $f_{\text{H}_1} n^2 \mathcal{R} = \frac{f_{\text{H}_2}}{2} n \int d\Omega \int_{\nu_1}^{\nu_2} d\nu \frac{I_{\nu}}{h\nu} \sigma_{\text{H}_2, \nu} f_{\text{diss}, \nu}$



$$f_{\text{H}_2} \simeq 1 - \frac{3}{4} \frac{s}{1 + 0.25s}$$

$$s = \frac{\ln(1 + 0.6\chi + 0.01\chi^2)}{0.6 \tau_c}$$

LW-shielding opacity
 $\tau_c = \Sigma_{\text{HI}} / \mu_{\text{H}} Z' \sigma'_d$

$$\chi = 71 \left(\frac{\sigma_{d, -21}}{\mathcal{R}_{-16.5}} \right) \frac{G'_0}{n_{\text{H}, 0}}$$

Ratio of the dust cross section per H nucleus to the rate coefficient of H₂ formation on dust grains ≈ 1

FUV intensity in units of the Milky Way's, $7.5 \times 10^{-4} \text{ cm}^{-3}$ (Draine 1978)

H₂-regulated Star Formation

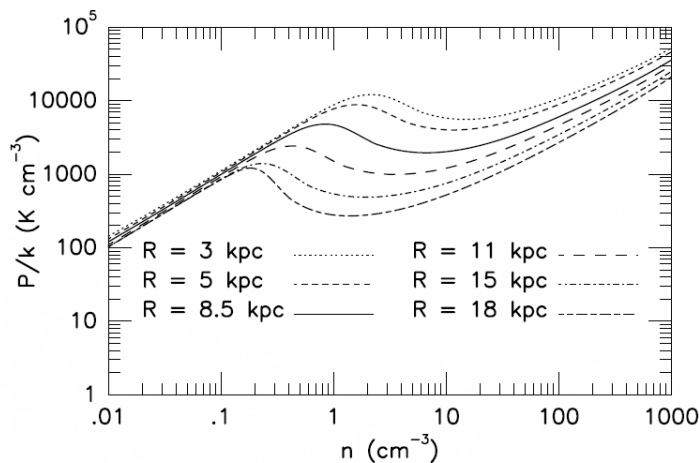
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With the assumption of 2-phase equilibrium between a Cold Neutral Medium and a Warm Neutral Medium, the minimum CNM density is proportional to the LW flux



Wolfire et al. (2003)

$$n_{\text{min}} \approx 31 G'_0 \frac{Z'_d / Z'_g}{1 + 3.1 (G'_0 Z'_d / \zeta'_t)^{0.365}} \text{ cm}^{-3},$$

and the KMT09 prescription for f_{H_2} becomes **independent of the LW intensity**.

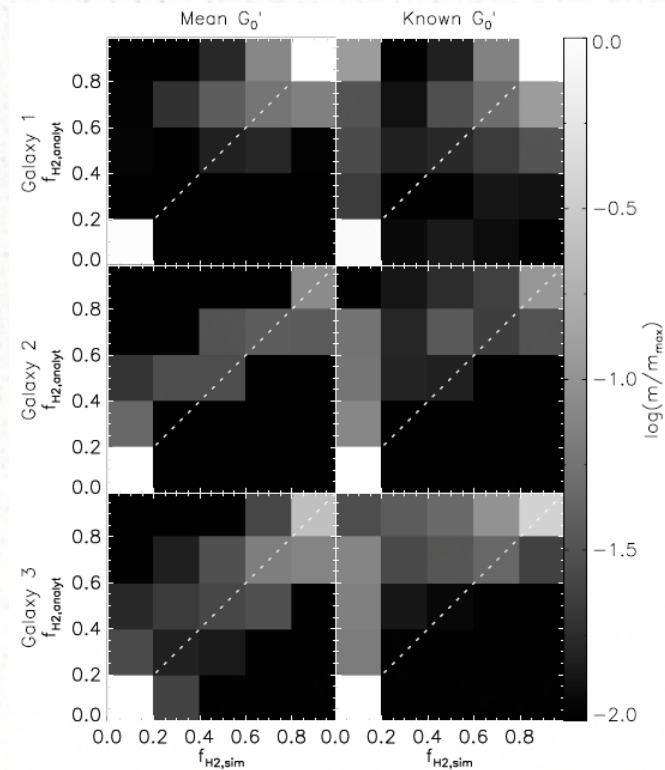
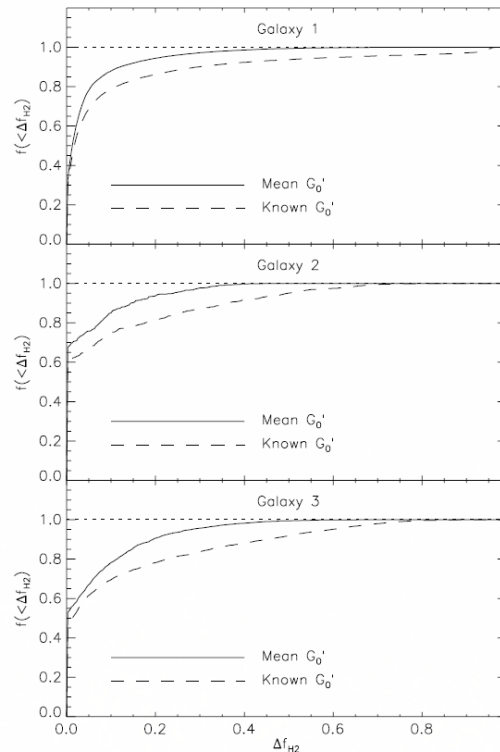
$$\chi = 2.3 \left(\frac{\sigma_{d,-21}}{\mathcal{R}_{-16.5}} \right) \frac{1 + 3.1 (Z/Z_{\text{SN}})^{0.365}}{\phi_{\text{CNM}}}$$

H₂-regulated Star Formation

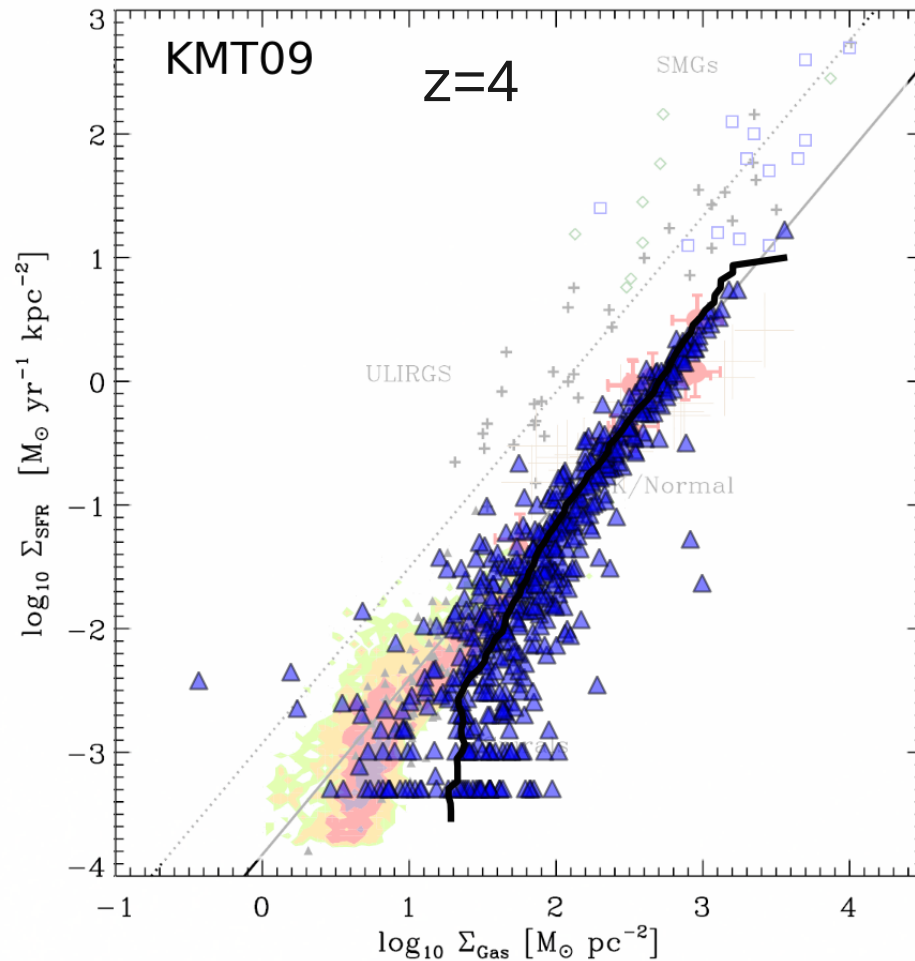
Krumholz & Gnedin (2010): direct comparison between self-consistent cosmological simulations (ART) and KMT09 model at z=3.

Simulations:

- Cosmological zoom-in simulations of 3 disk galaxies ($Z/Z_{\odot}=0.5, 0.01, 0.18$).
- Non-equilibrium chemical network with H₂ formation on dust (local Z).
- Star formation, metal enrichment, and “live” radiation transfer of ionizing radiation.
- LW shielding with Sobolev-like approximation: $S_D = e^{-D_{MW}\sigma_0(n_{HI} + 2n_{H_2})L_{Sob}}$ $L_{Sob} \equiv \rho/(2|\nabla\rho|)$



H₂-regulated Star Formation



Make SFR proportional to ρ_{H_2}
 No SF density threshold!

$$\dot{\rho}_{\text{SF}} = \epsilon_{\star} \frac{\rho_{\text{H}_2}}{t_{\text{freefall}}} \propto f_{\text{H}_2} \rho_{\text{gas}}^{3/2}$$

$$\epsilon_{\star} = 0.01$$

$$f_{\text{H}_2} \simeq 1 - \frac{3}{4} \frac{s}{1 + 0.25s}$$

$$s = \frac{\ln(1 + 0.6\chi + 0.01\chi^2)}{0.6 \tau_c}$$

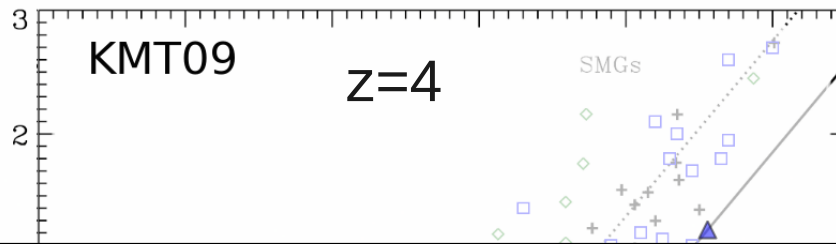
$$\chi = 0.77 (1 + 3.1 Z'^{0.365})$$

$$\tau_c = \Sigma_{\text{HI}} / \mu_{\text{H}} Z' \sigma'_d$$

$10^{-3} Z_{\odot}$ metallicity floor at $z=10$.

Further metal enrichment from SN injection: $0.25 M_{\star}$, yield=0.02.

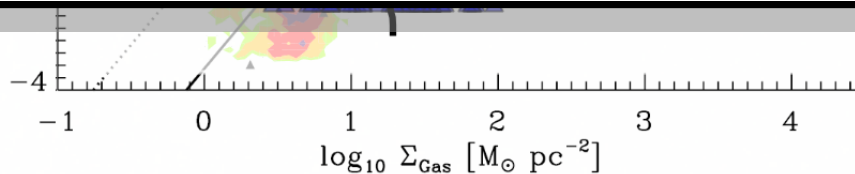
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Name	z_{final}	$\rho_{\text{gas,SF}}$	n_{thresh}	$J_{\text{LW}}/J_{\text{MW}}$	$[Z_{\text{floor}}]$	Comment
KT07	4.0	tot	50 cm^{-3}	—	—	Krumholz & Tan (2007) SF law
KT07_low	6.0	tot	5 cm^{-3}	—	—	lower SF threshold
KT07_high	6.0	tot	500 cm^{-3}	—	—	higher SF threshold
KMT09	4.0	H ₂	—	—	-3.0	Krumholz et al. (2009): 2-phase equilibrium
KMT09_L8	6.0	H ₂	—	—	-3.0	one additional refinement level (maxlevel=8)
KMT09_FLW1	5.0	H ₂	—	1	-3.0	KMT09 with uniform LW
KMT09_FLW10	5.0	H ₂	—	10	-3.0	background of
KMT09_FLW100	5.0	H ₂	—	100	-3.0	increasing
KMT09_FLW1000	5.0	H ₂	—	1000	-3.0	intensity
KMT09_ZF4.0	6.0	H ₂	—	—	-4.0	lower Z_{floor}
KMT09_ZF2.5	6.0	H ₂	—	—	-2.5	higher Z_{floor}
KMT09_ZF2.0	6.0	H ₂	—	—	-2.0	even higher Z_{floor}
KMT09_ZFz10	6.0	H ₂	—	—	-3.0	Z_{floor} at $z = 10$

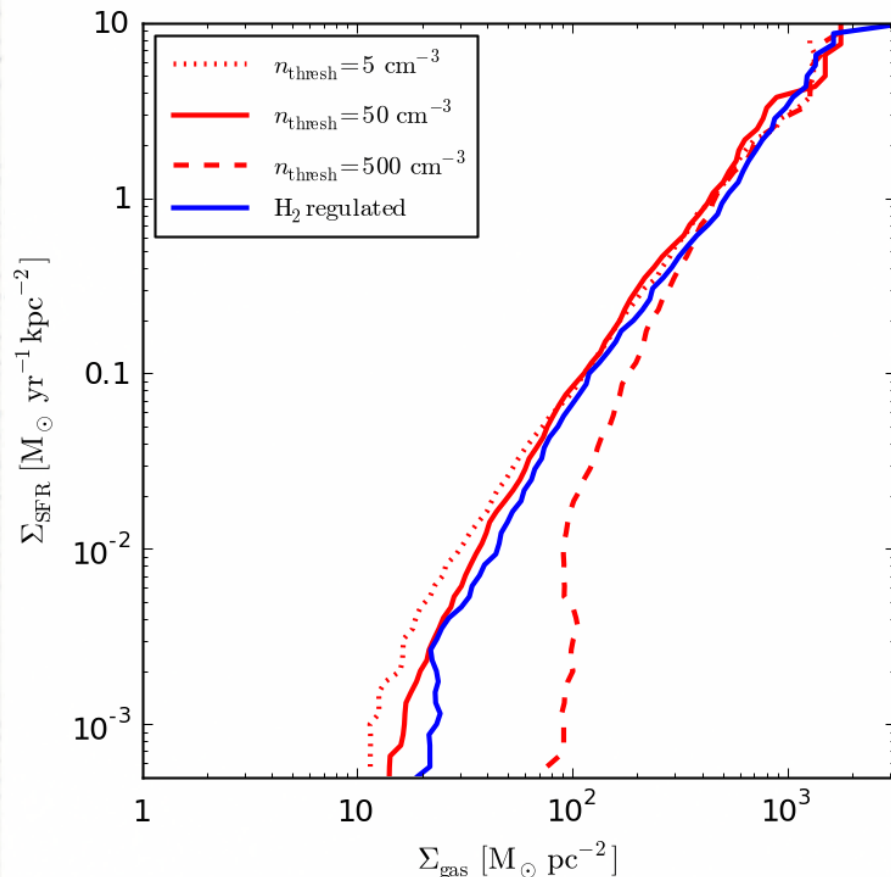


$10^{-3} Z_{\odot}$ metallicity floor at $z=10$.

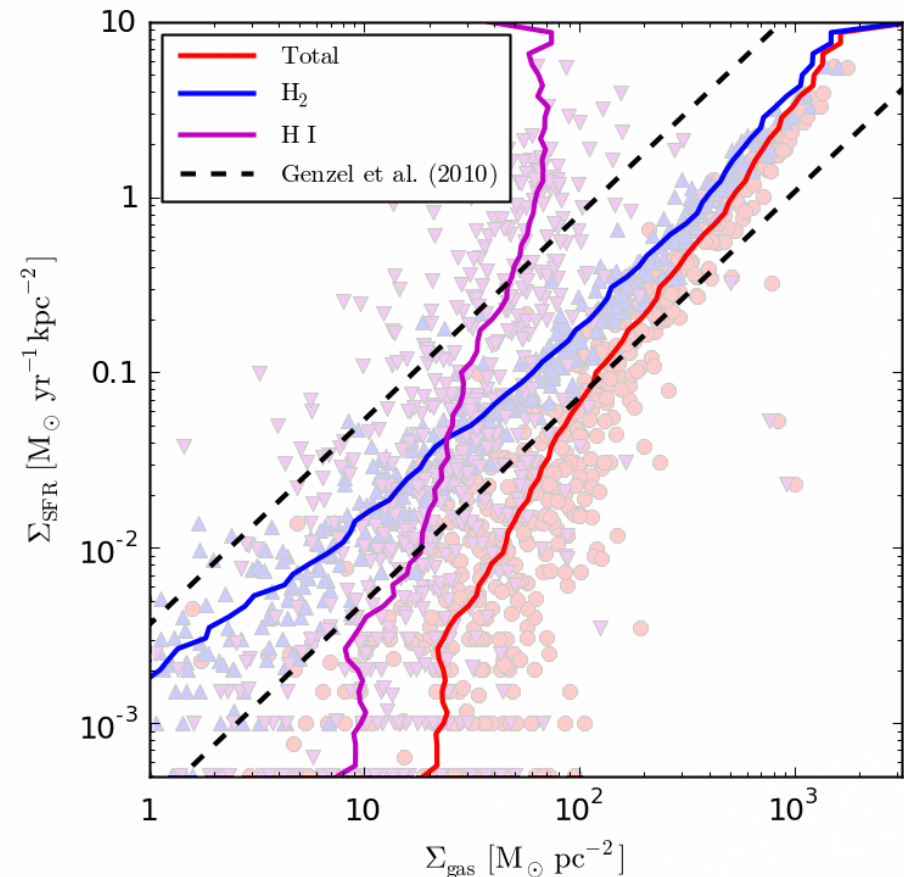
Further metal enrichment from SN injection: $0.25 M_{\star}$, yield=0.02.

Comparisons with observational SF scaling laws

See also: Gnedin, Tassis, & Kravtsov (2009), Gnedin & Kravtsov (2010, 2011), Feldmann & Gnedin (2010)



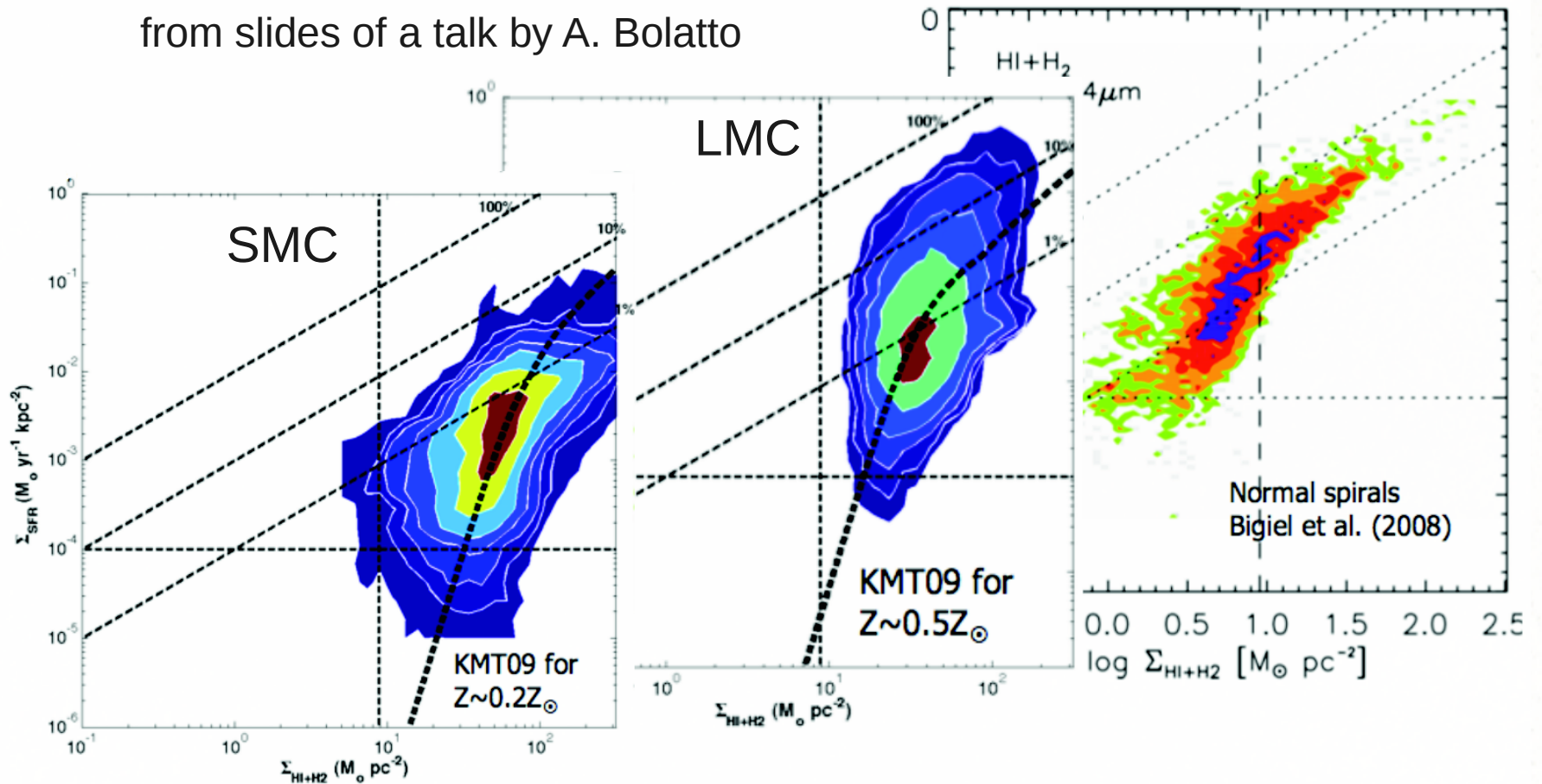
The H_2 -regulated model reproduce the turnover in Σ_{SFR} without an artificial density threshold.



The H_2 -KS relation lies between the Genzel et al. (2010) $z=0 - 3.5$ relations for "normal" and "luminous mergers".

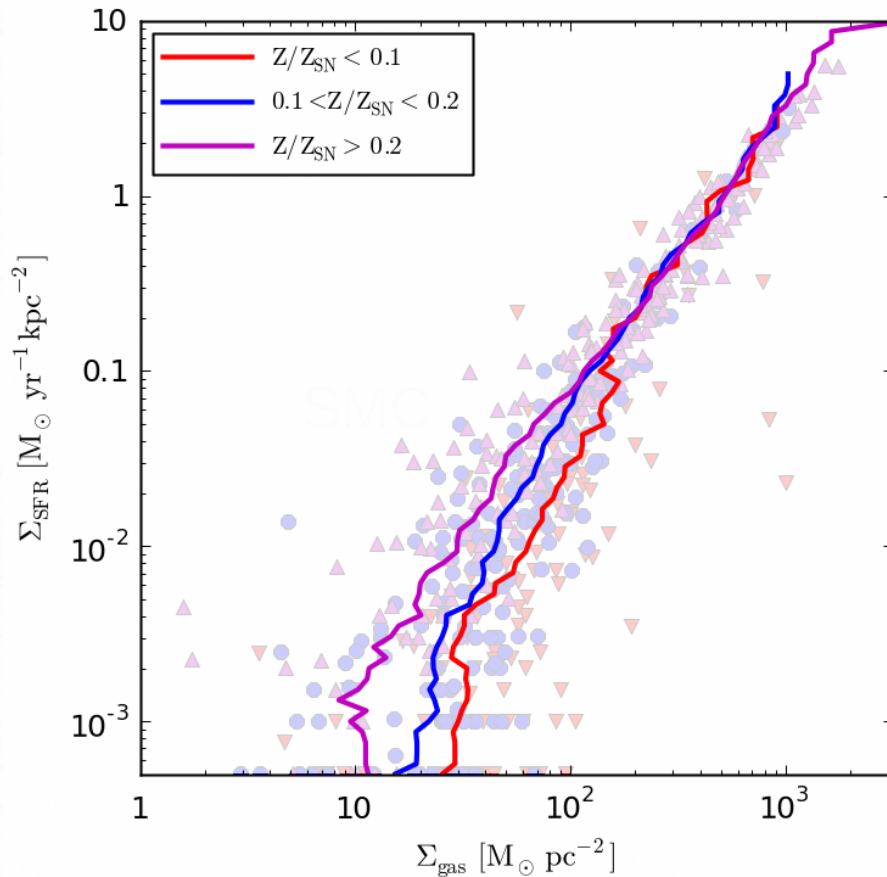
Metallicity Dependence

from slides of a talk by A. Bolatto

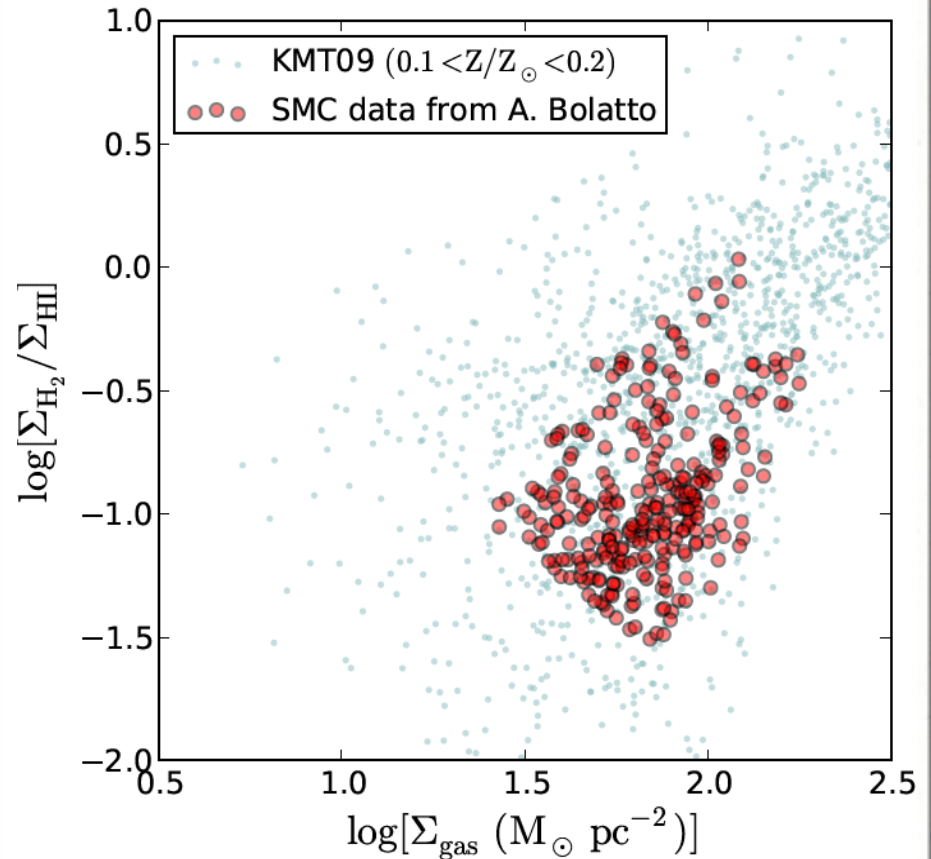


see also Bolatto et al. (2011, arXiv:1107.1717)

Metallicity Dependence



Our model is able to capture the metallicity-dependence of the rollover in the KS relation.



H_2 fractions as a function of total Σ_{gas} compare favorably with recent direct measurements in the SMC (Bolatto et al. 2011, arXiv:1107.1717).

H₂-regulated Star Formation

Example halo in KT07 simulation:

$$M_{\text{tot}} = 1.86 \times 10^{10} M_{\odot}$$

$$M_{\text{gas}} = 2.43 \times 10^9 M_{\odot}$$

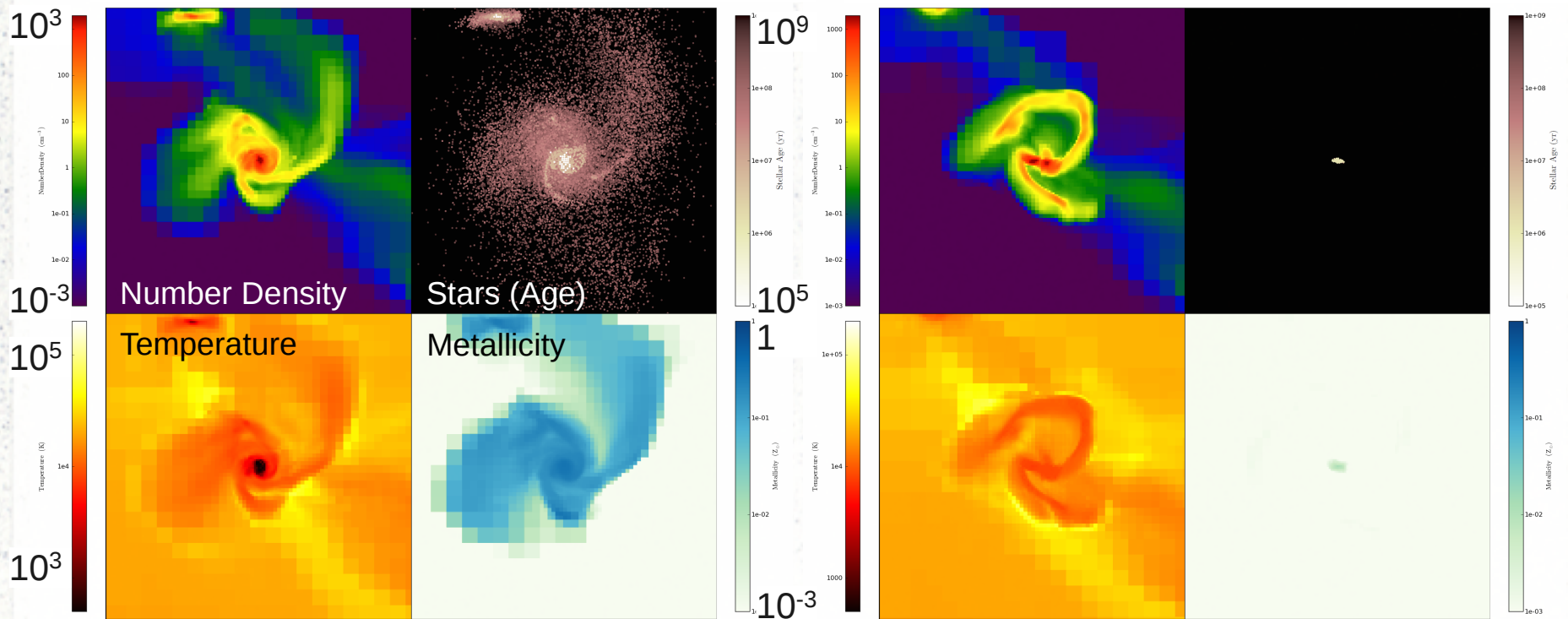
$$M_{\star} = 1.16 \times 10^9 M_{\odot}$$

Same halo in KMT09 simulation:

$$M_{\text{tot}} = 1.83 \times 10^{10} M_{\odot}$$

$$M_{\text{gas}} = 3.43 \times 10^9 M_{\odot}$$

$$M_{\star} = 1.46 \times 10^7 M_{\odot}$$



H₂-regulated Star Formation

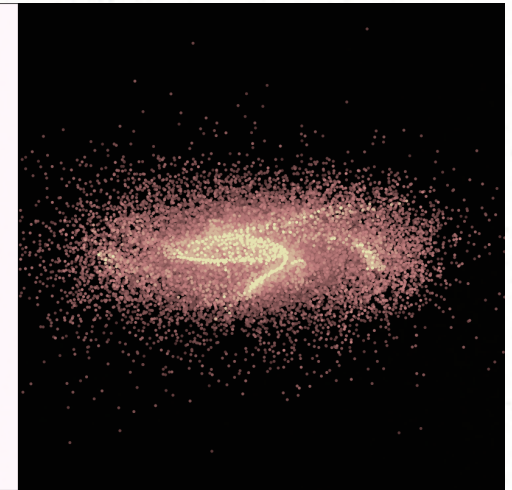
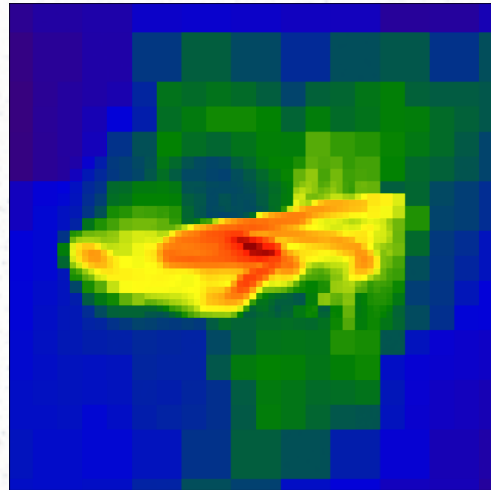
High Mass Halo:

$$M_{\text{tot}} = 2.8 \times 10^{10} M_{\odot}$$

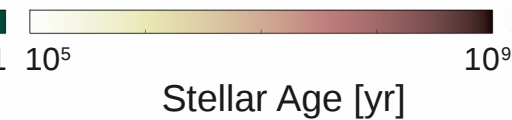
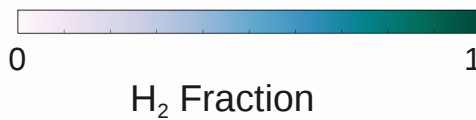
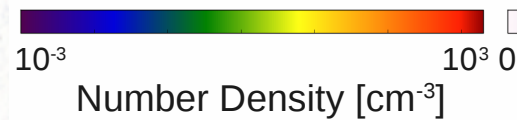
$$M_{\text{gas}} = 3.0 \times 10^9 M_{\odot}$$

$$M_{\star} = 2.4 \times 10^9 M_{\odot}$$

$$f_{\star} = 8.6 \times 10^{-2}$$



Both KMT09



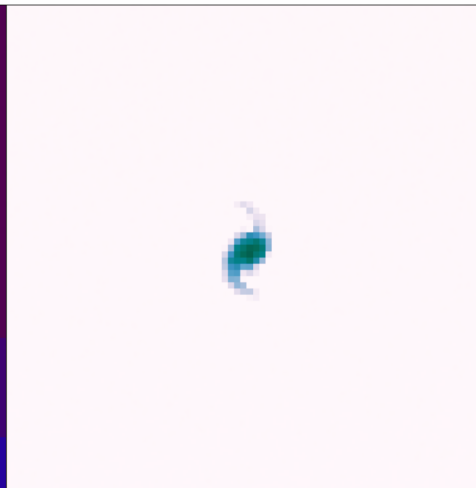
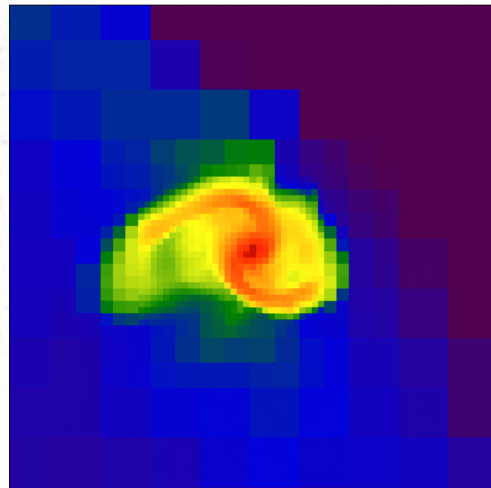
Low Mass Halo:

$$M_{\text{tot}} = 4.7 \times 10^9 M_{\odot}$$

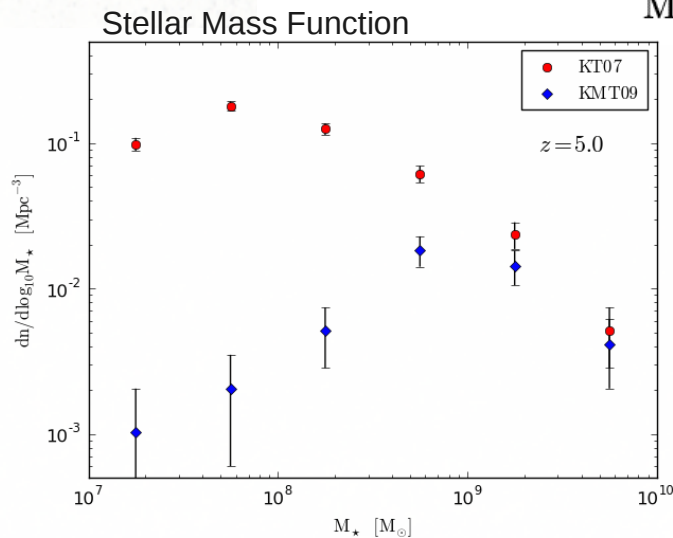
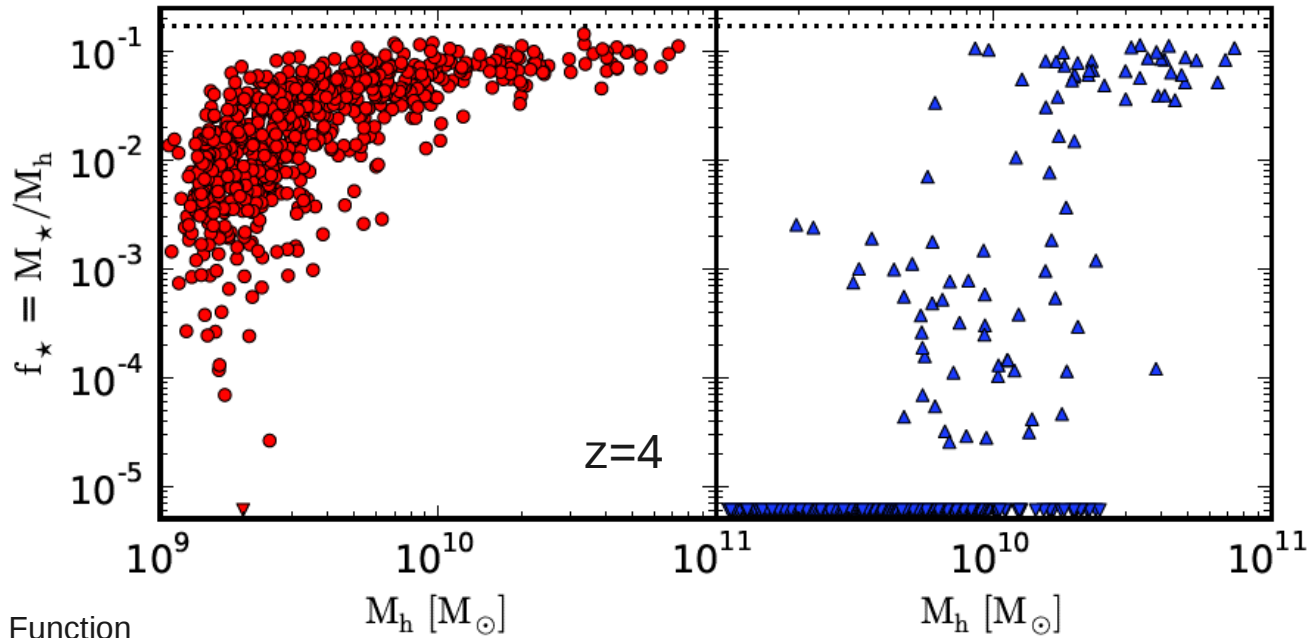
$$M_{\text{gas}} = 7.8 \times 10^8 M_{\odot}$$

$$M_{\star} = 5.7 \times 10^7 M_{\odot}$$

$$f_{\star} = 1.2 \times 10^{-2}$$

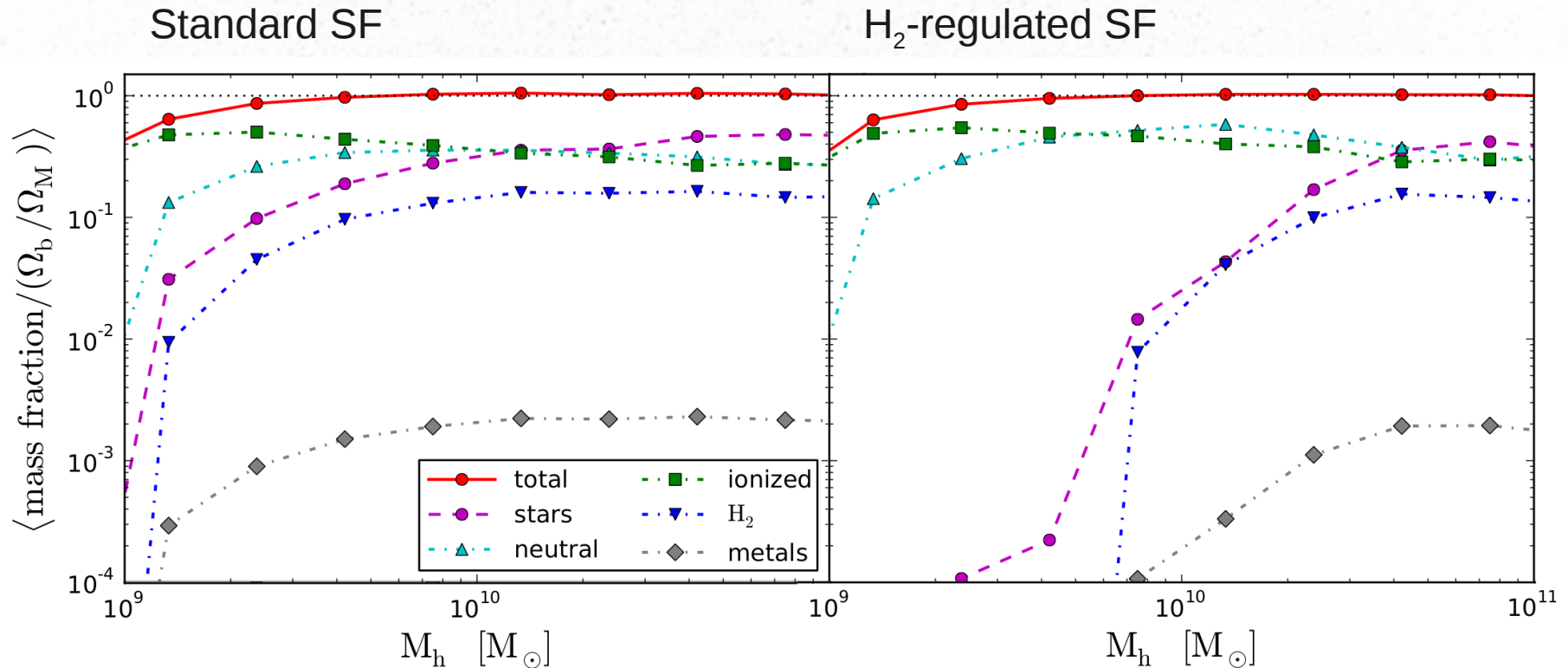


H₂-regulated Star Formation



Regulating star formation by the H₂ abundance greatly reduces the star formation efficiency in low mass halos. This helps to resolve the **Dwarf Galaxy Problems**.

Baryon Content

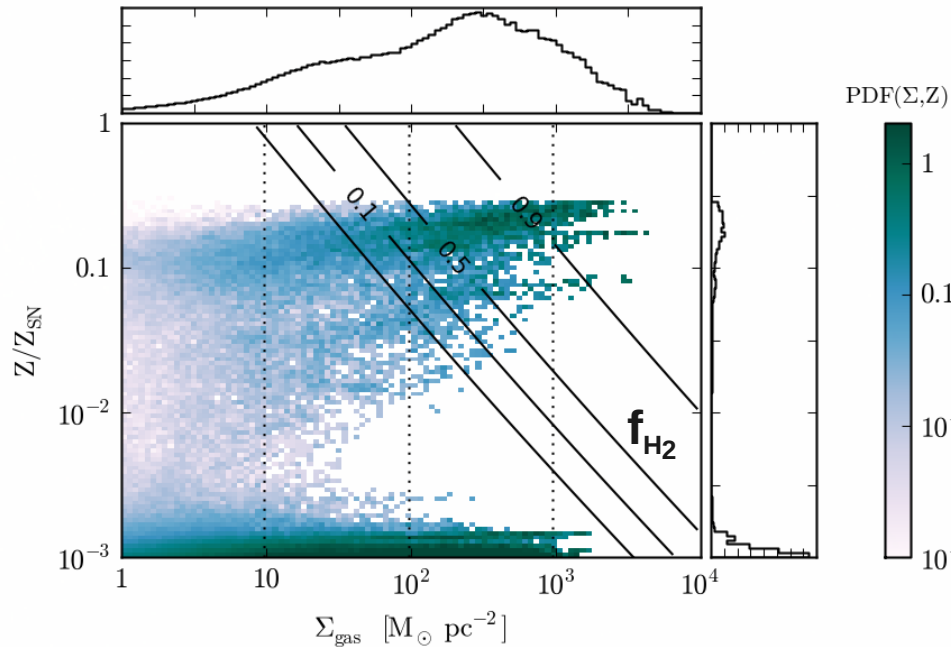


Lower mass halos have lower star formation efficiency ($f_* = M_*/M_{\text{tot}}$) owing to their **lower metallicity**.

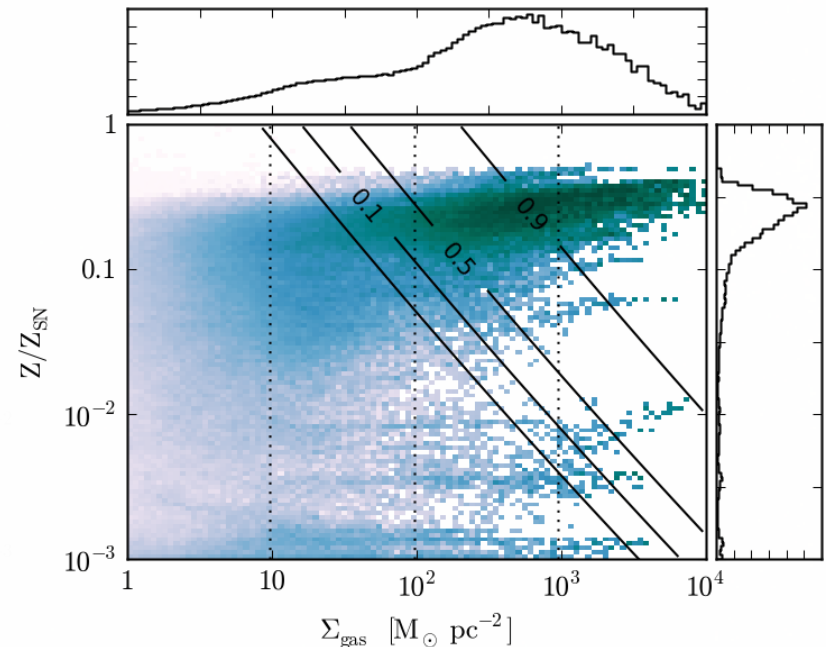
Lower $Z \Rightarrow$ Less Lyman-Werner shielding \Rightarrow Smaller $f_{H_2} \Rightarrow$ Reduced star formation

Halo Mass Dependence of f_{\star}

Low Mass Halos ($M < 10^{10} M_{\odot}$)



High Mass Halos ($M > 10^{10} M_{\odot}$)



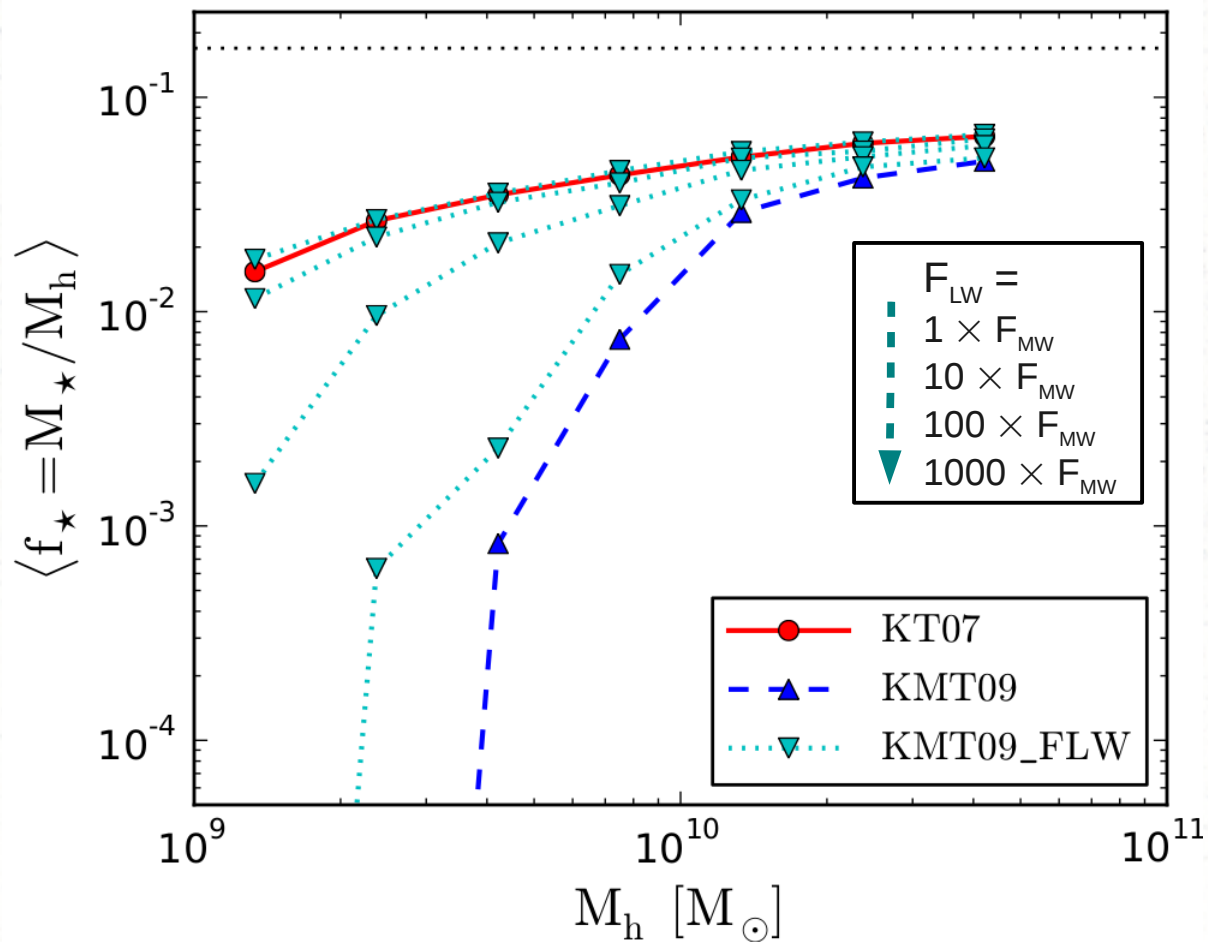
Lower mass halos have lower star formation efficiency ($f_{\star} = M_{\star}/M_{\text{tot}}$) owing to their **lower metallicity**.

Lower $Z \Rightarrow$ Less Lyman-Werner shielding \Rightarrow Smaller $f_{\text{H}_2} \Rightarrow$ Reduced star formation

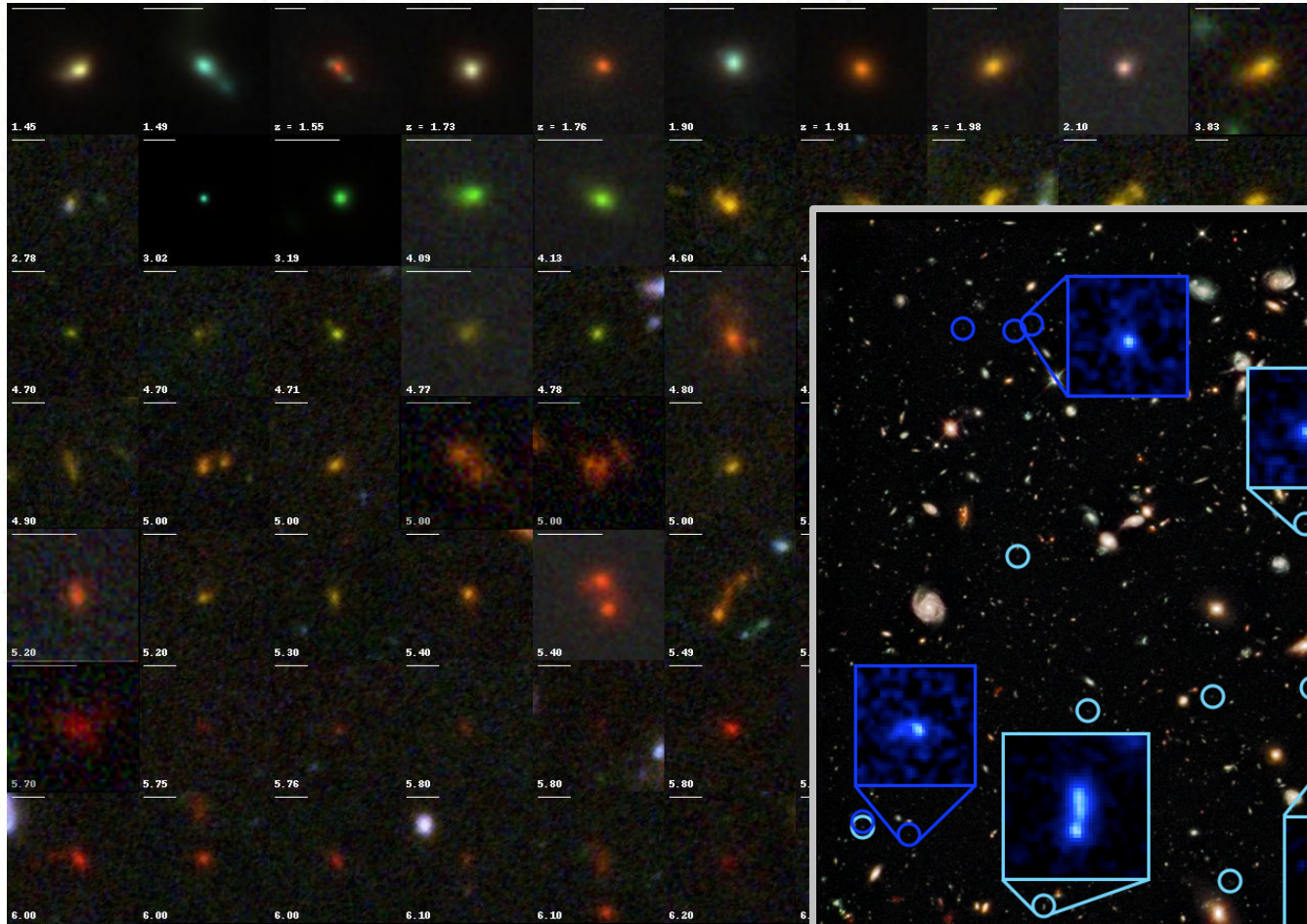
H₂-regulated Star Formation

Without the 2-phase equilibrium assumption the f_{\star} -suppression mass scale depends on the strength of the LW background.

[It also becomes dependent on a subgrid clumping factor, set to 30 here (Krumholz & Gnedin 2010).]

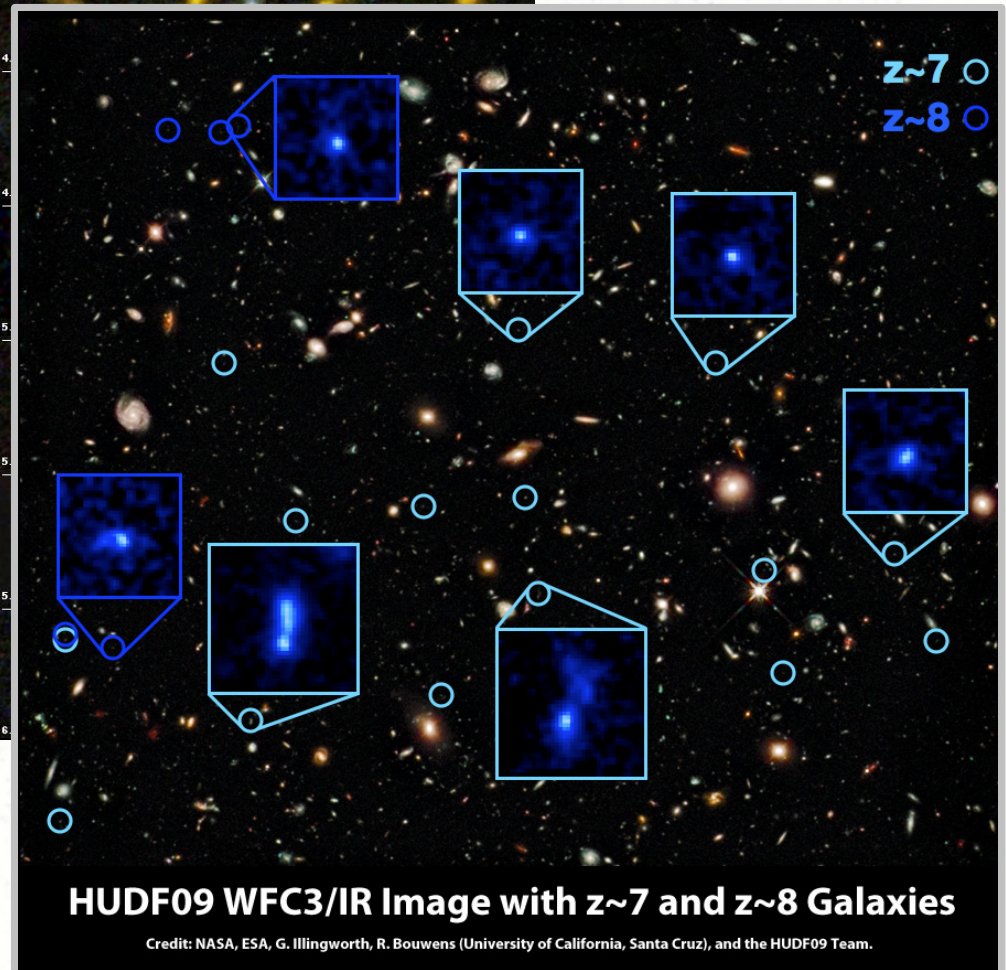


Comparison with high-z observations

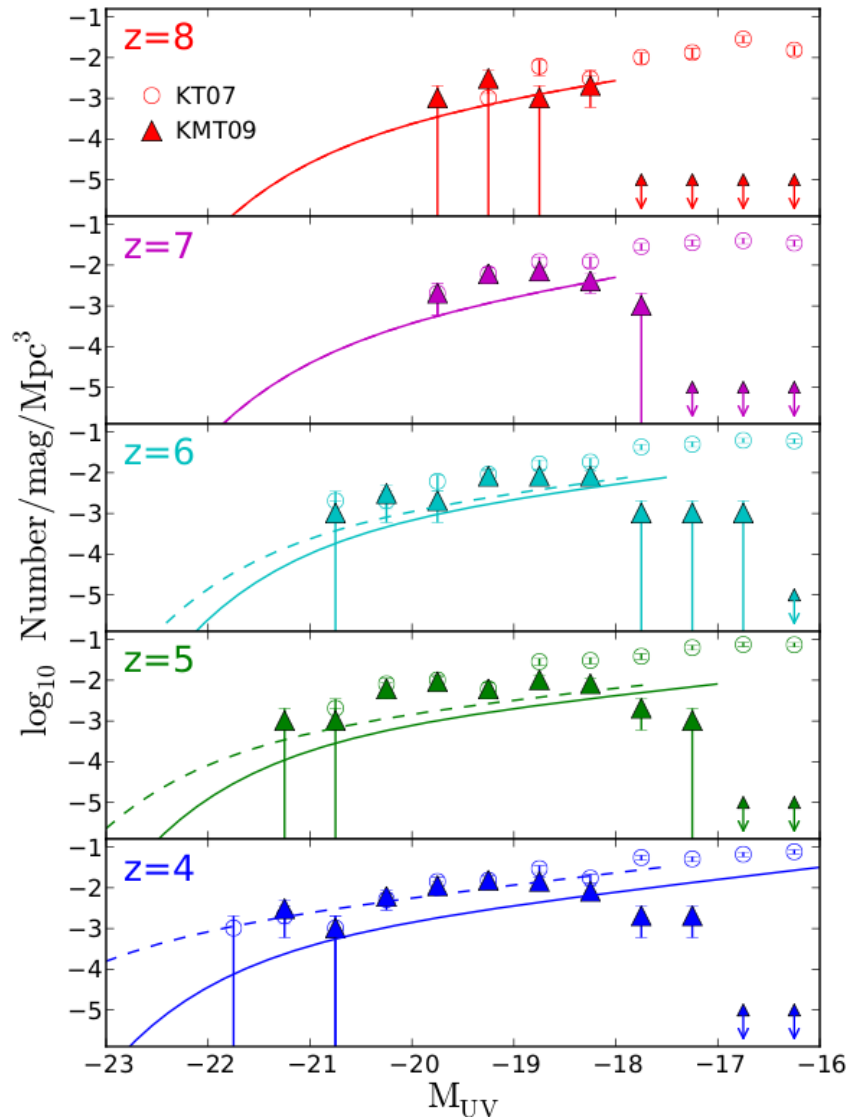


Malhotra et al. (HUDF-GRAPES)

Illingworth et al.
(HUDF09)



H₂-regulated Star Formation



Observational luminosity functions from Bouwens et al. 2007, 2010.

Dust corrections very important!

[Bouwens et al. 2010:

1.55, 0.625, 0.375, 0, 0 mags at z = 4, 5, 6, 7, 8.]

We calculate L_{UV} from SFR:

$$L_{UV} = 8.0 \times 10^{27} (\text{SFR}/M_{\odot} \text{ yr}^{-1}) \text{ erg s}^{-1} \text{ Hz}^{-1}$$

Standard SF overpredicts LF.

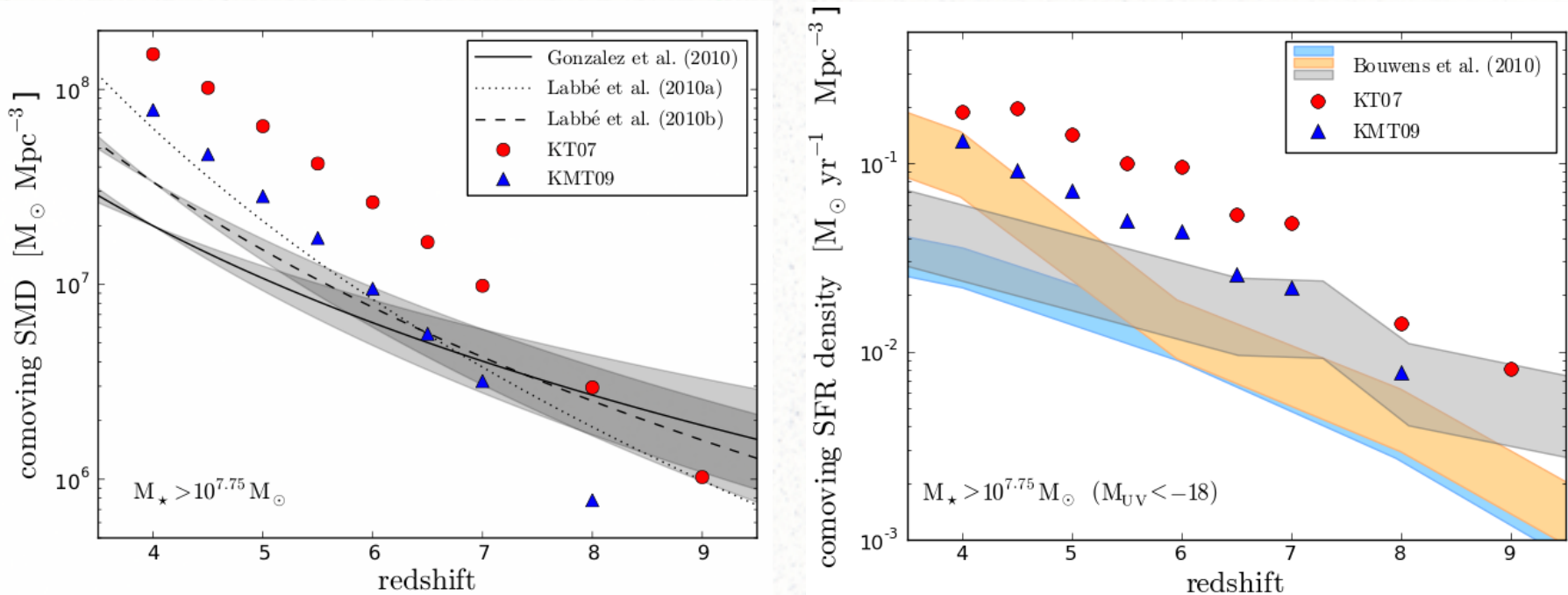
[except at z=4?]

H₂-regulated SF improves agreement around sensitivity limit ($M_{UV}=-18$).

H₂ suppression in this realization may be too strong for fainter systems.

H₂-regulated Star Formation

Evolution of Stellar Mass Density... and ...Star Formation Rate Density



Compares favorably with current (uncertain!) determinations utilizing ultra-deep rest-frame UV HST ACS/WFC3 observations coupled with stellar masses estimated from Spitzer rest-frame optical measurements.

[Bouwens et al. 2009, 2010, Gonzalez et al. 2010, Labbé et al. 2009, 2010, Stark et al. 2009]

Conclusions

- There are **two dwarf galaxy problems** in our understanding of the galaxy formation process:
 - 1) The Missing Satellites Problem
 - 2) The Field Dwarf Galaxy Problem
- Both are typically explained by invoking “supernova feedback”, but other explanations should be considered. One example is **H₂-regulated star formation**.
- Cosmological **AMR hydrodynamical galaxy formation simulations** with Enzo show that regulating SF by the H₂ abundance:
 - Reproduces the cutoff in Σ_{SFR} in the Kennicutt-Schmidt relation at $\sim 10 M_{\odot}/\text{pc}^2$ without the need for a SF density threshold.
 - Matches the observed H₂-KS relation as reported by Genzel et al. (2010) at $z=0-3.5$.
 - Suppresses star formation in $M < 10^{10} M_{\odot}$ halos, because these galaxies aren't able to self-enrich as well as more massive halos.
 - Improves the agreement with (uncertain) observational determinations of the cosmic stellar mass density and SFR density evolution at $z > 4$.
 - **Helps to alleviate the dwarf galaxy problems.**